



**GENERAL DYNAMICS**  
Ordnance and Tactical Systems

Prepared by

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Prepared for

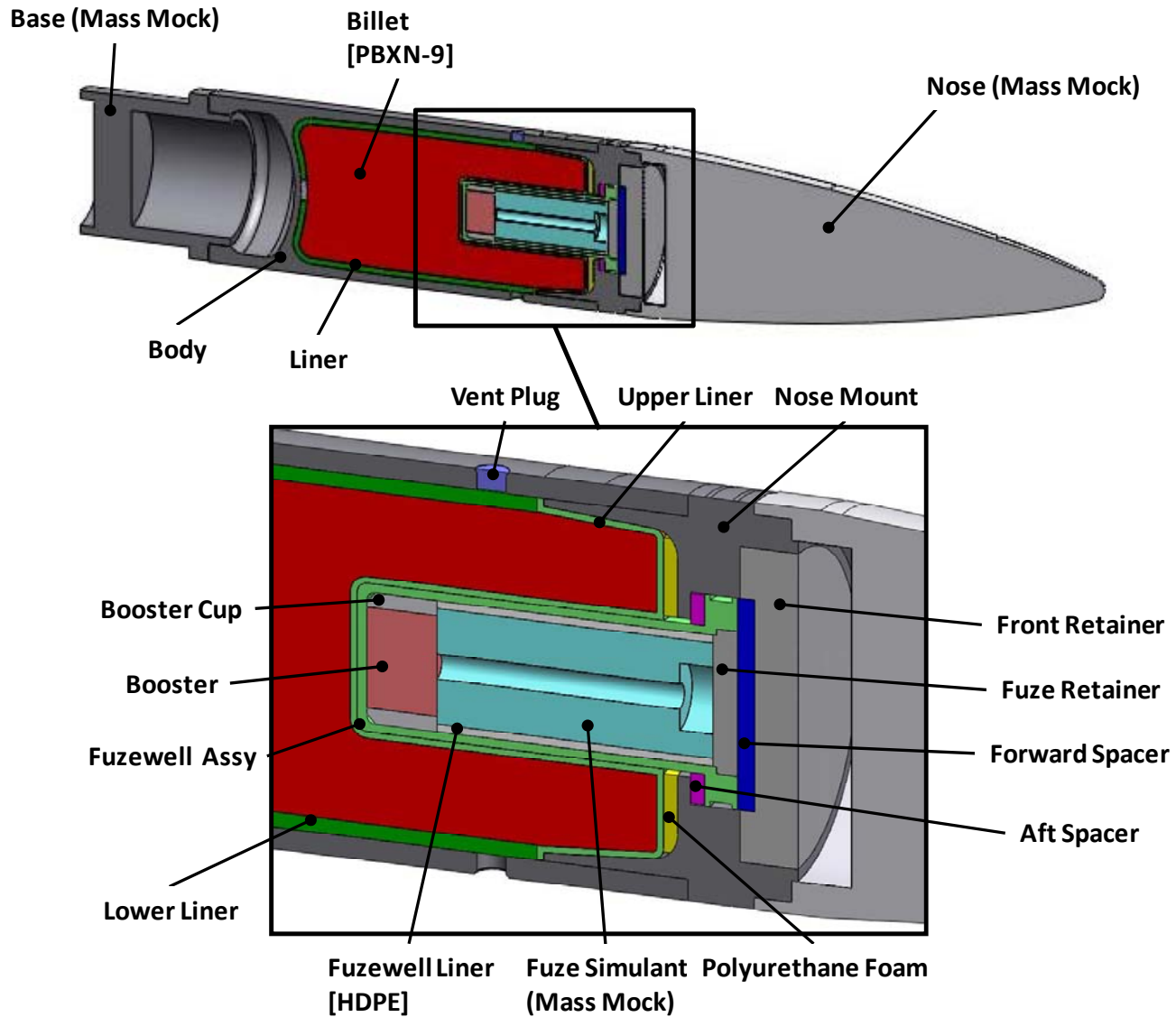
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***TECHNOLOGY DRIVEN. WARFIGHTER FOCUSED.***

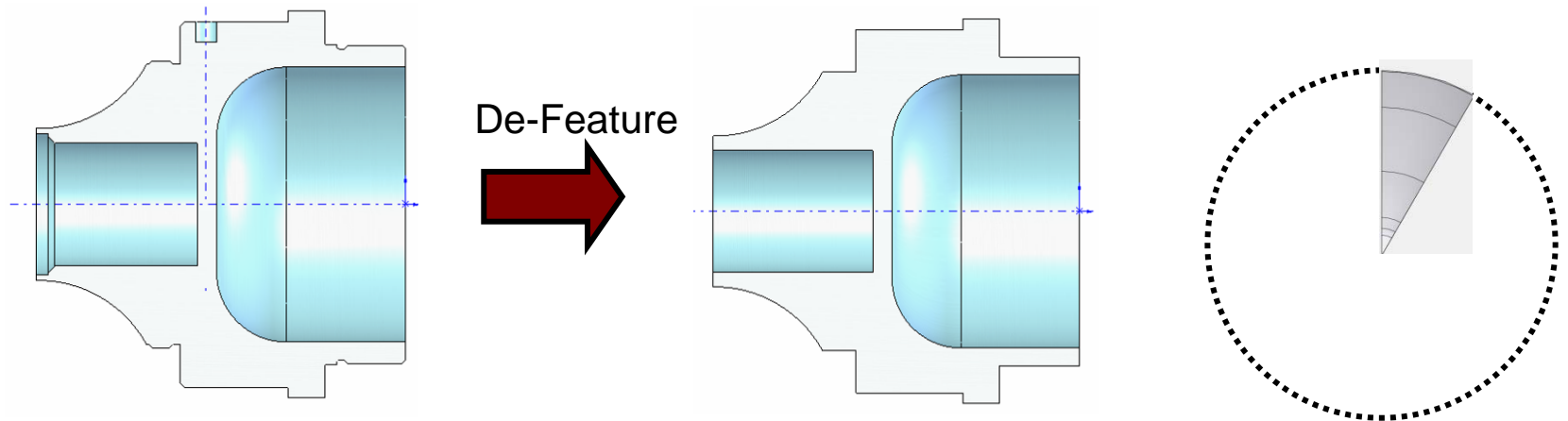
## **Modeling Methodology for Predicting SCO Performance of the Excalibur Warhead**

- The objective of this presentation is to describe a thermal modeling methodology used to analyze Slow Cook-Off in the Excalibur Warhead
- Modeling Goals are as follows:
  - To gain understanding of heat transfer in the Excalibur warhead when exposed to slow heating environment
  - Use this understanding to design mitigation methods that ensure the Excalibur warhead burns (Type V Reaction) during slow heating environment



- Steps used for thermal modeling and analysis
  - De-Feature Model
  - Apply Contact Resistances
  - Define Material Properties
  - Define Thermal Loads and Constraints
  - Run Thermal Model
  - Compare Model to test results

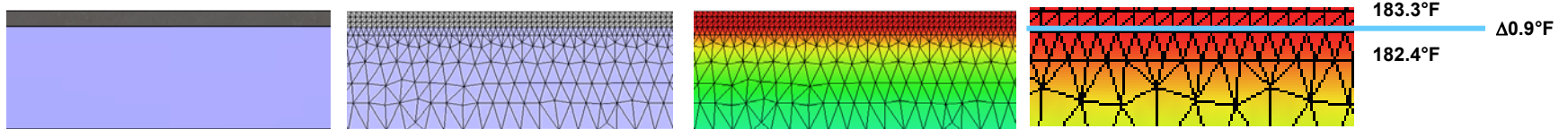
- “De-featuring” a solid model means parts are simplified or combined in an effort to reduce computational size of the model.
  - Assemblies made from the same material can be combined
  - Features such as fillets and chamfers are eliminated
  - Symmetry used where possible
    - Use “wedges” on axisymmetric parts or assemblies



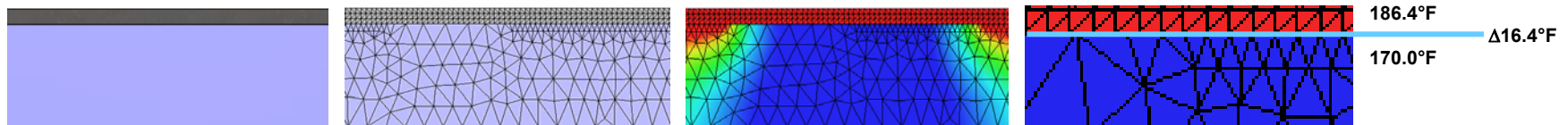
- Presence of gaps caused by tolerances can change how heat transfers across material interfaces
- Contact resistances can be applied between surfaces
  - Interfaces must be line to line
  - Resistance value calculated based on gap thickness and thermal conductivity of filler material (air, RTV, etc.)
    - Gap Thickness =  $t$  [m]
    - Thermal Conductivity =  $k$  [W/m•K]
    - Contact Resistance =  $t/k$  [K•m<sup>2</sup>/W]
    - Resistance increases as gap thickness increases
    - Resistance increases as thermal conductivity decreases

- The three cases below illustrate how interface conditions can change thermal transfer
  - One hour calculation with convection applied to upper surface

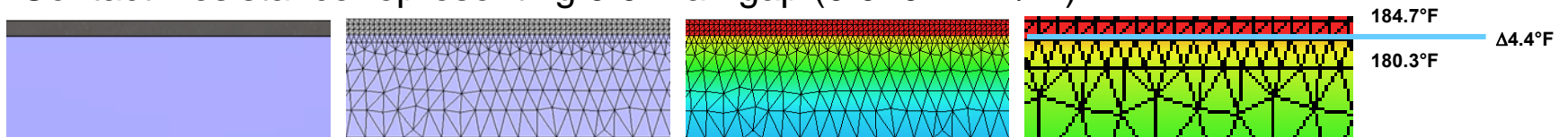
A perfect, line-to-line interface between two parts allows for ideal heat transfer



Accidentally putting in a gap can change the heat transfer across the interface



Contact Resistance representing 0.01" air gap (0.010 m<sup>2</sup>•K/W)



- Material properties required for thermal model:
  - Density
  - Thermal Conductivity
  - Specific Heat
  - Kinetic Constants
    - Activation Energy
    - Pre-Exponential Factor
    - Heat of Reaction



- Basic Material Properties are input as constants or as a function of temperature
  - Density
  - Thermal Conductivity
  - Specific Heat
- Material properties for explosive formulations are not always published so the Rule of Mixtures can be applied based on the component materials

$$k = \sum (f_i \cdot k_i) = f_1 k_1 + f_2 k_2 + \dots + f_i k_i$$

$$f_1 = \frac{\frac{wt\%_1}{\rho_1}}{\frac{wt\%_1}{\rho_1} + \frac{wt\%_2}{\rho_2} + \dots + \frac{wt\%_i}{\rho_i}}, \quad f_2 = \frac{\frac{wt\%_2}{\rho_2}}{\frac{wt\%_1}{\rho_1} + \frac{wt\%_2}{\rho_2} + \dots + \frac{wt\%_i}{\rho_i}}, \text{ etc...}$$

$k$  = thermal conductivity of each component

$f$  = volume fraction of each component

wt% = weight percentage of each component

$\rho$  = density of each component

- An Arrhenius rate equation is used to calculate the self-heating properties of the explosive as a function of temperature
- Activation Energy, Heat of Reaction and Pre-Exponential Factor are the kinetic constants
- Activation Energy and Pre-Exponential factor must be calculated by ASTM-E 698-05, if not published
  - Standard Test Method for Arrhenius Kinetic Constants for Thermally Unstable Materials Using Differential Scanning Calorimetry and the Flynn/Wall/Ozawa Method

$$\text{Heat Rate} = \rho Q Z e^{-E/RT}$$

$\rho = \text{Density}$

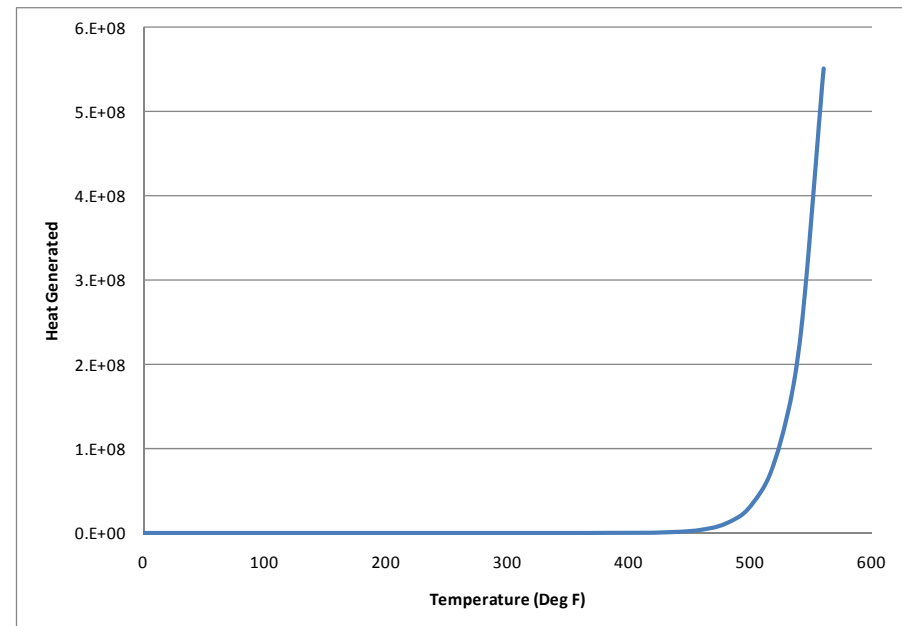
$Q = \text{Heat of Reaction}$

$Z = \text{Pre-Exponential Factor}$

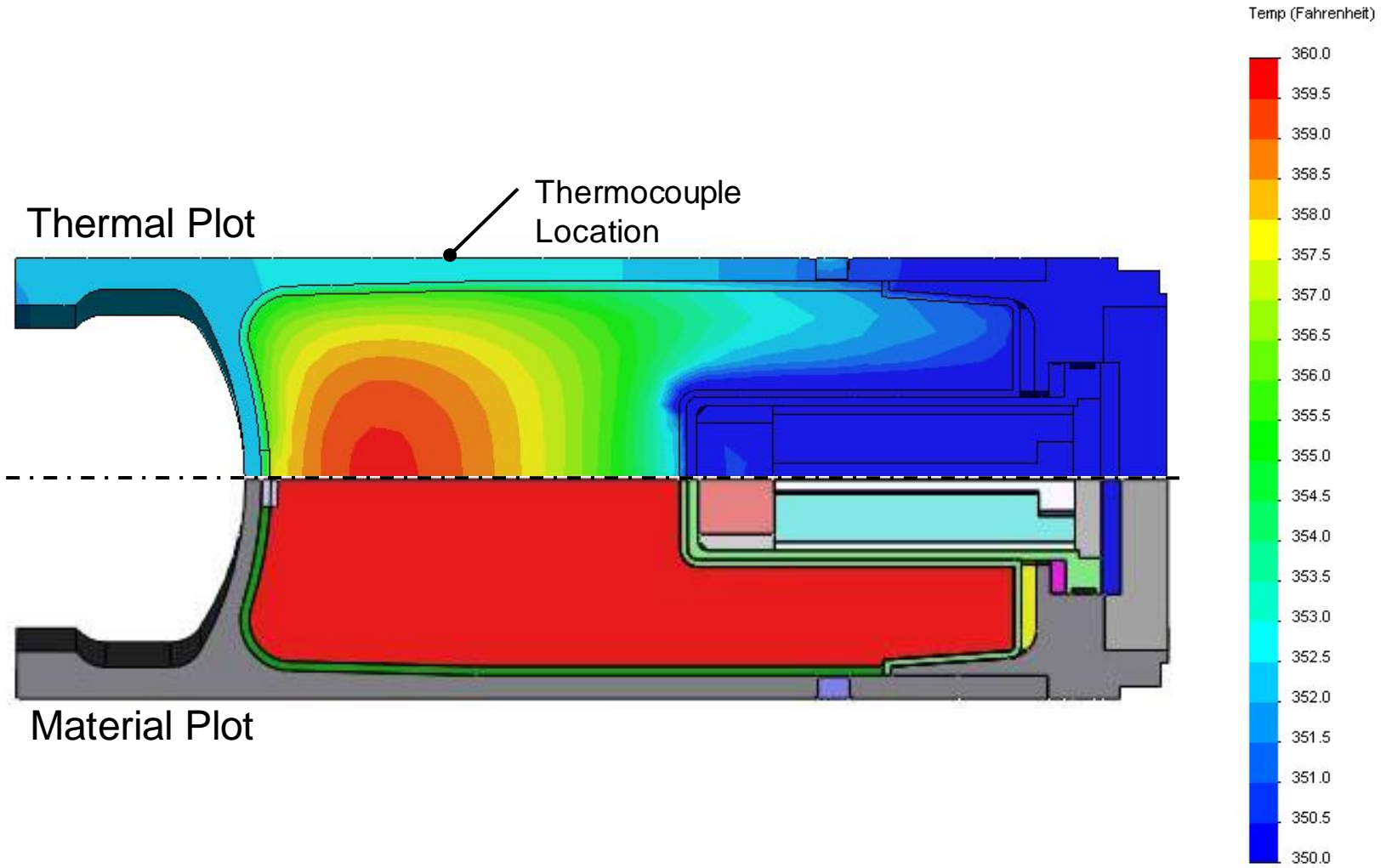
$E = \text{Activation Energy}$

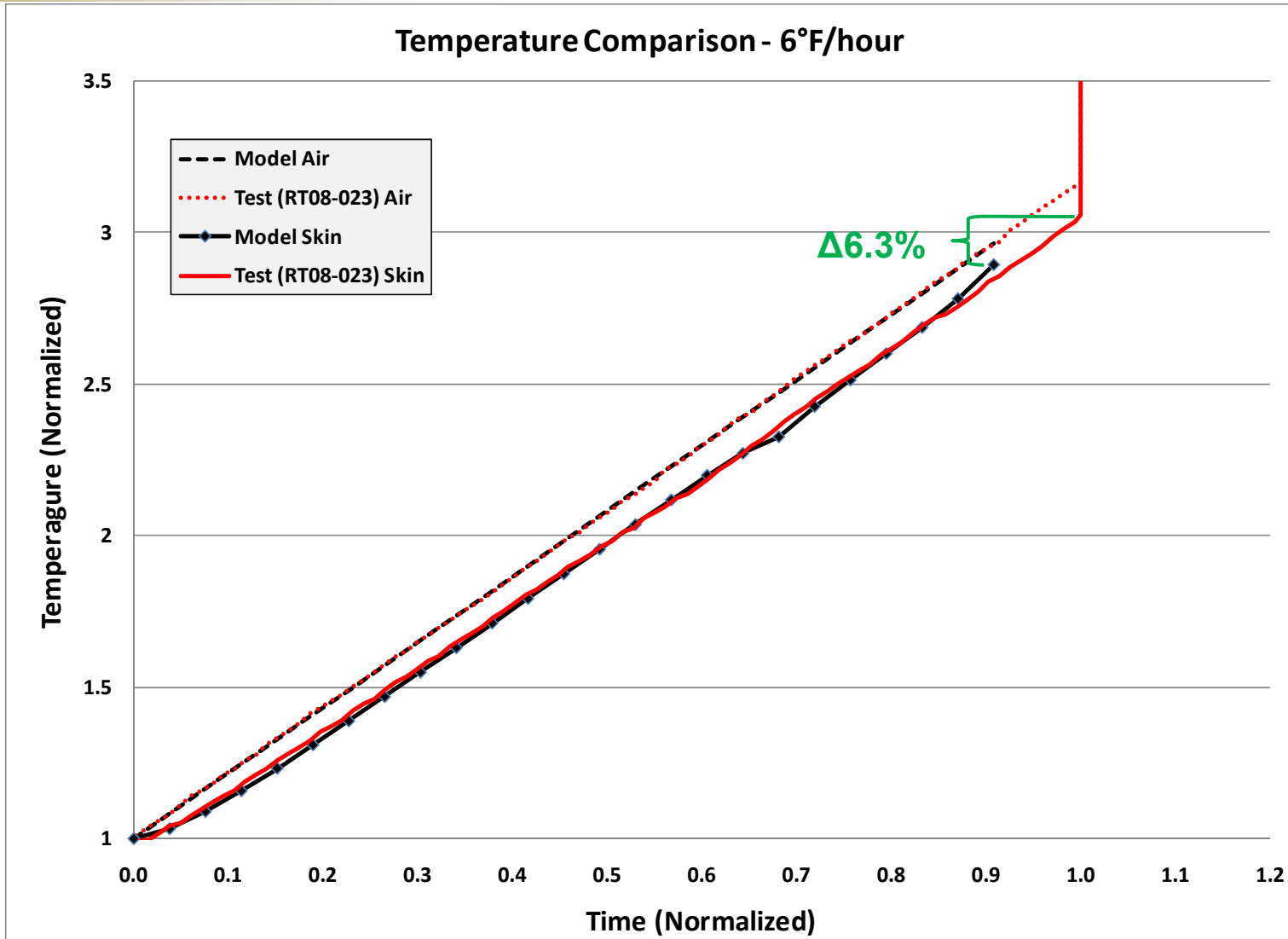
$R = \text{Universal Gas Constant}$

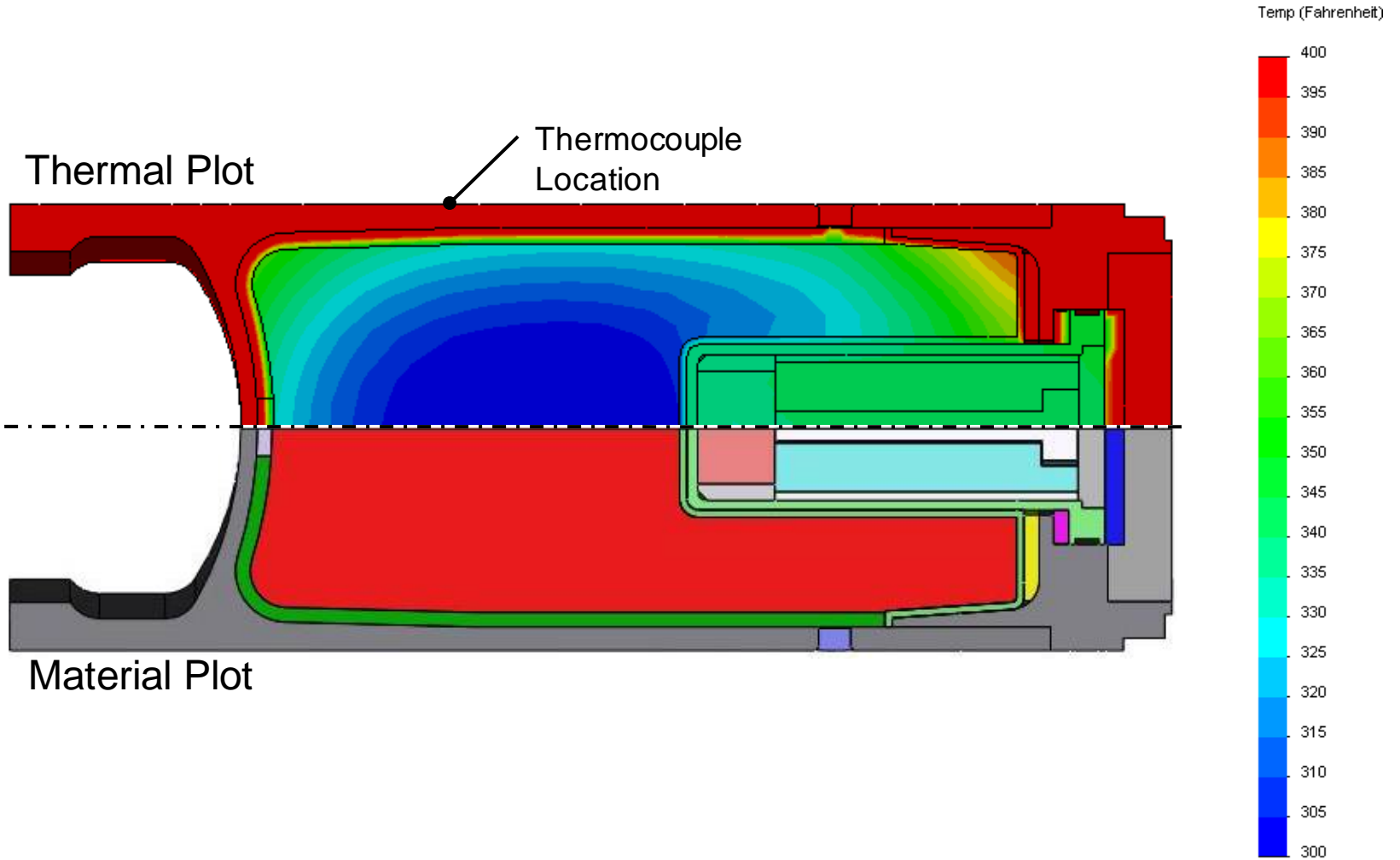
$T = \text{Absolute Temperature}$

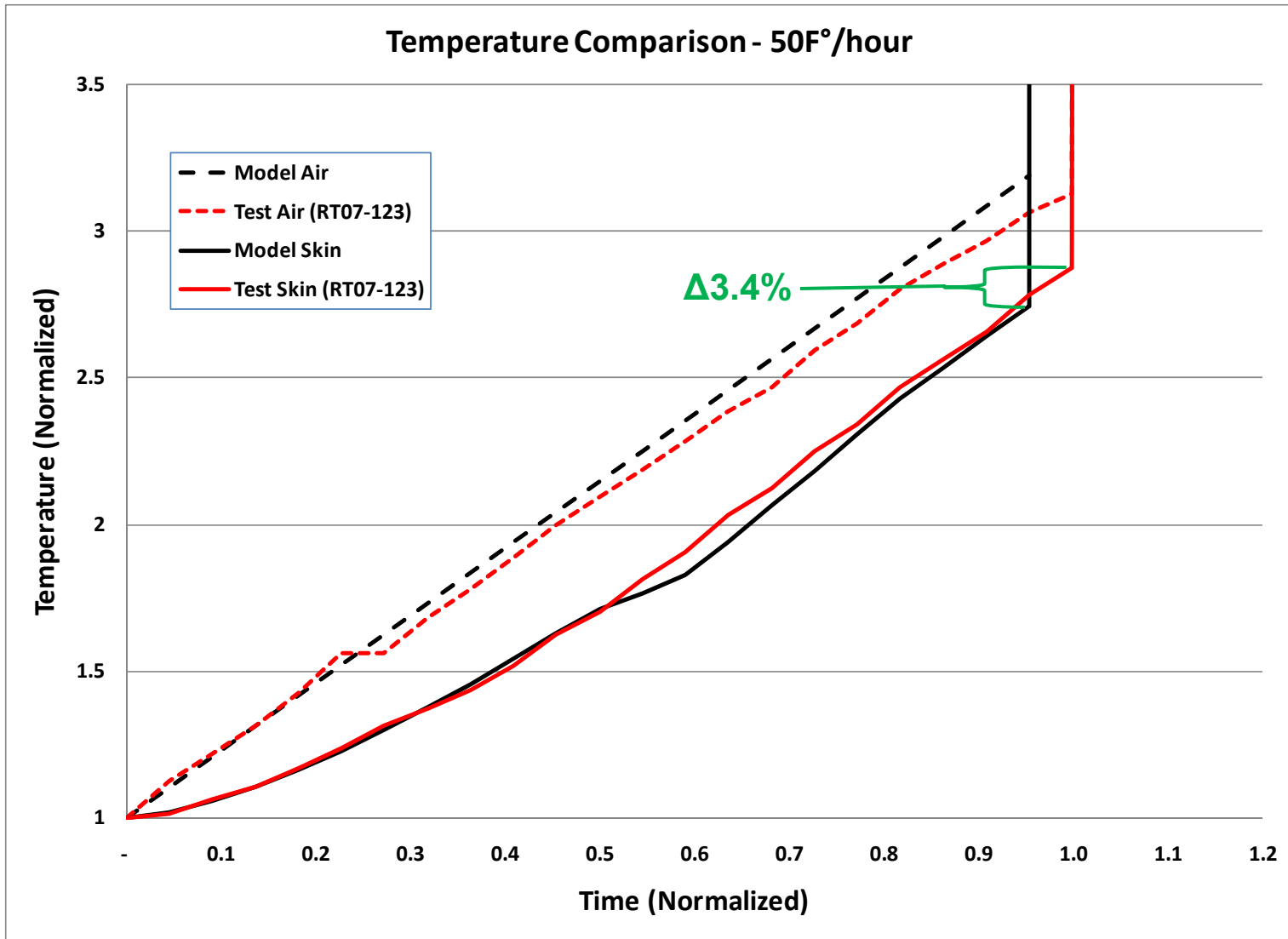


- The initial temperature of all components is the start temperature to be used during SCO tests
  - 122°F most common
- Convection is applied to all surfaces that will be exposed to moving air within the oven.
  - Convection Coefficient: 12 W/m<sup>2</sup> K
  - Bulk Temperature of convective medium heated at 50°/hour or 6°/hour, depending on test conditions intended for study
- Self heating properties of explosive applied as heat power generated as a function of temperature









- Conclusions
  - A standard methodology has been developed for predicting SCO reaction times and temperatures
    - Accurate within 7% at 6°F/hour heat rate on Excalibur
    - Accurate within 4% at 50°F/hour heat rate on Excalibur
  - Method can be applied to other systems
- Future Work
  - Continue to gather test data and compare to models
  - Develop burn models to calculate what happens after reaction takes place
    - Models only predict reaction time and temperature, not Type



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