





Promoting National Security Since 1919



## Raising the Bar: Equipping DoD Testers to Excel with DOE

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- Test design is not an art...it is a science
  - Talented scientists in T&E Enterprise however...limited knowledge in test design...alpha, beta, sigma, delta, p, & n
- Our decisions are too important to be left to professional opinion alone...our decisions should be based on <u>mathematical fact</u>
- **53d Wg, AFOTEC, AFFTC, and 46 TW/AAC experience** 
  - Teaching DOE as a sound test strategy not enough
  - Leadership from senior executives (SPO & Test) is key
- Purpose: DOD adopts experimental design as the default approach to test, wherever it makes sense
  - Exceptions include demos, lack of trained testers, no control







- B.S. US Naval Academy, Engineering Operations Analysis
- M.S. Stanford University, Operations Research
- USAF Officer -- TAWC Green Flag, AFOTEC Lead Analyst
- Consultant -- Booz Allen & Hamilton, Sverdrup Technology
- Mathematics Chief Scientist -- Sverdrup Technology
- Wing OA and DOE Champion 53<sup>rd</sup> Wing, now 46 Test Wing
- USAF Reserves Special Assistant for Test Methods (AFFTC/CT) and Master Instructor in DOE for USAF TPS

### **Practitioner, Design of Experiments -- 19 Years**

Selected T&E Project Experience – 18+ Years

Green Flag EW Exercises '79	SCUD Hunting '91
F-16C IOT&E '83	AGM-65 IIR '93
AMRAAM, JTIDS ' 84	MK-82 Ballistics '94
NEXRAD, CSOC, Enforcer '85	Contact Lens Mfr '95
Peacekeeper '86	Penetrator Design '96
B-1B, SRAM, '87	30mm Ammo '97
MILSTAR '88	60 ESM/ECM projects '98'00
MSOW, CCM '89	B-1B SA OUE, Maverick IR+, F-15E
Joint CCD T&E '90	Suite 4E+,100's more '01-'06





# Systems Engineering Employ Many Simulations of Reality



		Simulation of Reality						
Acq Phase		M&S		Hardware		System/Flight Test		
Reqt'ts Dev								
	AoA							
Concepts							Drototypo	
	<b>Risk Reduction</b>	Warfare	Physics				FIOLOLYPE	
EMD			FILYSICS	HWIL/SIL	Captive	Subsystem	Drod Pop	
	Prod & Mfr						riou nep	
Sustain							Production	

- At each stage of development, we conduct experiments
  - Ultimately how will this device function in service (combat)?
  - Simulations of combat differ in fidelity and cost
  - Differing goals (screen, optimize, characterize, reduce variance, robust design, trouble-shoot)
  - Same problems distinguish truth from fiction: What matters? What doesn't?



### DOE in Action: Six Sigma at General Electric

- Fortune Global 2000 #1 in 2009 based on Sales, Profit, Assets and Market Value (\$180B, \$17B, \$800B, \$90B)
- Climate Brand Index #1
- Global Most Admired Company Fortune 2005 #1 or #2 last 10 years
- Global Most Respected Barron's top 15 consistently
- Recognized globally as one of the best for for innovation, investor relations, reporting, working mothers, ethics, accountability
- Products and Services
  - Aircraft engines, appliances, financial services, aircraft leasing, equity, credit services, global exchange services, NBC, industrial systems, lighting, medical systems, mortgage insurance, plastics







## GE's (Re)volution In Improved Product/Process



- Began in late 1980's facing foreign competition
- 1998, Six Sigma Quality becomes one of three company-wide initiatives
- '98 Invest \$0.5B in training; Reap \$1.5B in benefits!
- "Six Sigma is embedding quality thinking process thinking across every level and in every operation of our Company around the globe"<sup>1</sup>
- "Six Sigma is now the way we work in everything we do and in every product we design" <sup>1</sup>

Jack Welch 
General Electric website at ge.com

### **DOE in Historical Stats Timeline**<sup>1</sup>

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1800	Least Squares (Gauss, Legendre)
1850	
1900	Regression Concepts (Pearson, Galton)
1910	t-test (Gosset)
1920	Factorial Experiments and ANOVA (Fisher)
1930	Formalized Hypothesis Tests and Power (Neyman, Pearson)
1940	2 <sup>k</sup> Factorial Designs (Yates) Fractional Factorial Designs (Finney, Rao)
1950	Taguchi develops his methods Central Composite, Response Surface Methods (RSM) Designs (Box, Wilson)
1960	Optimal Designs (Kiefer, Wolfowitz) Box-Behnken Designs (Box, Behnken)
1970	2 <sup>k-p</sup> Fractional Factorial Resolution (Box, Hunter)
1980	Algorithm for D-optimal designs (Mitchell, Nachtsheim)
1990	Detecting dispersion effects ratio of variances (Montgomery)
2000	53 Wing Starts using DOE

1. Source: Appendix K -- Understanding Industrial Designed Experiments, Schmidt and Launsby, 1998







- Four Challenges The JPADS Drop Test
- What's the BEST strategy of test?
- DOE Fables for the T&E Enterprise
- How can we deploy DOE to revolutionize Test?
- Summary



## What are Statistically Designed Experiments?





- Purposeful, systematic changes in the inputs in order to observe corresponding changes in the outputs
- Results in a mathematical model that predicts system responses for specified factor settings

$$\mathsf{Responses} = f(\mathsf{Factors}) + \varepsilon$$



### Why DOE? One Slide... DOE Gives Scientific Answers to Four

**Fundamental Test Challenges** 



- Four Challenges faced by any test
  - 1. How many? <u>Depth</u> of Test effect of test size on uncertainty
  - 2. Which Points? <u>Breadth</u> of Testing spanning the vast employment battlespace
  - 3. *How Execute?* <u>Order</u> of Testing insurance against "unknownunknowns"
  - What Conclusions? Test <u>Analysis</u> drawing objective, scientific conclusions while controlling noise





## A beer and a blemish ...





- 1906 W.T. Gossett, a Guinness chemist
- Draw a yeast culture sample
- Yeast in this culture?
- Guess too little incomplete fermentation; too much -- bitter beer
- He wanted to get it right



- 1998 Mike Kelly, an engineer at contact lens company
- Draw sample from 15K lot
- How many defective lenses?
- Guess too little mad customers; too much -- destroy good product
- He wanted to get it right



# Today's Example – Precision Air Drop System





- Just when you think of a good class example – they are already building it!
- 46 TS 46 TW Testing JPADS

The dilemma for airdropping supplies has always been a stark one. High-altitude airdrops often go badly astray and become useless or even counter-productive. Low-level paradrops face significant dangers from enemy fire, and reduce delivery range. Can this dilemma be broken?

A new advanced concept technology demonstration shows promise, and is being pursued by U.S. Joint Forces Command (USJFCOM), the U.S. Army Soldier Systems Center at Natick, the U.S. Air Force Air Mobility Command (USAF AMC), the U.S. Army Project Manager Force Sustainment and Support, and industry. The idea? Use the same GPS-guidance that enables precision strikes from JDAM bombs, coupled with software that acts as a flight control system for parachutes. JPADS (the Joint Precision Air-Drop System) has been combat-tested successfully in Iraq and Afghanistan, and appears to be moving beyond the test stage in the USA... and elsewhere.

### Capability:

Assured SOF re-supply of material Requirements: Probability of Arrival Unit Cost \$XXXX Damage to payload Payload Accuracy Time on target Reliability ...

# Challenge #1 ... How Many?

- In all our testing we reach into the bowl (reality) and draw a sample of JPADS performance
- Consider an "80% JPADS"
  - Suppose a required 80% P(Arrival)
  - Is the Concept version acceptable?
- We don't know in advance which bowl God hands us ...
  - The one where the system works or,
  - The one where the system doesn't







Start -- Blank Sheet of Paper: How Many?



- Let's draw a sample of <u>n</u> drops
- How many is enough to get it right?
  - 3 because that's how much \$/time we have
  - 8 because I'm an 8-guy
  - 10 because I'm challenged by fractions
  - 30 because something good happens at 30!

### Let's start with 10 and see ...

=> Switch to Excel File – JPADS Pancake.xls



## Embedded Excel Simulation to Address "How Many?"



#### **Definitions:**

 $\alpha$  - false positive error rate - concluding a difference exists (good or bad) when the difference is noise. *Confidence* is 1- $\alpha$ .

 $\beta$ -false negative error rate - failing to detect a difference when a difference is causally-based *Power* is 1- $\beta$ .

We replicate to overcome sampling error but fail to quantify the *uncertainty* in our estimates.







- Suppose we fail JPADS when it has 4 or more misses
- We'll be wrong (on average) about 10% of the time
- We can tighten the criteria (fail on 7) by failing to field more good systems
- We can loosen the criteria (fail on 5) by missing real degradations
- Let's see how often we miss such degradations ...

In this bowl – JPADS performance is acceptable





### A false negative – we field JPADS (when it's degraded) -- β



- Use the failure criteria from the previous slide
- If we *field* JPADS with 6 or fewer hits, we fail to detect the degradation
- If JPADS has degraded, with n=10 shots, we're wrong about 65% of the time
- We can, again, tighten or loosen our criteria, but at the cost of increasing the other error

In this bowl – JPADS P(A) *decreased* 10% -- it is degraded





## We seek to balance our chance of errors



- Combining, we can trade one error for other (α for β)
- We can also increase sample size to decrease our risks in testing
- These statements not opinion –<u>mathematical fact</u> and an inescapable challenge in testing
- There are two other ways out ... factorial designs and real-valued MOPs



Enough to Get It Right: *Confidence* in stating results; *Power* to find small differences



### Challenge 2: Which Points? How Designed Experiments Solve This



**Designed Experiment** (n). Purposeful <u>control</u> of the inputs (factors) in such a way as to <u>deduce</u> their <u>relationships</u> (if any) with the <u>output</u> (responses).



### Statistician G.E.P Box said ...

"All math models are false ...but some are useful." "All experiments are designed ... most, poorly."



# Battlespace Conditions for JPADS Case



		Туре	Measure of Performance		
	Systems Engineering Question: Does JPADS perform at required capability level across the planned battlespace?         Conditions       Settings         PADS Variant:       A, B, C, D         .aunch Platform:       C-130, C-17, C-5         .aunch Opening       Ramp, Door         Farget:       Plains, Mountain         Cime of Day:       Dawn/Dusk, Mid-Day         Environment:       Forest, Desert, Snow         Weather:       Clear (+7nm), Haze (3-7nm), Low Ceiling/Visibility (<3000/3nm)	Objective	Target acquisition range		
			Target Standoff (altitude)		
Systems			launch range		
			mean radial arrival distance		
perform			probability of damage		
planned		<u> </u>			
•		Subjective			
			numan factors		
Conditions	Cottingo	#1 0.0010	support equipment		
	Settings	# Leveis	tactics		
JPADS Variant:		4			
Launch Platform:	C-130, C-17, C-5	3			
Launch Opening	Ramp, Door	2			
Target:	Plains, Mountain	2			
Time of Day:	Dawn/Dusk, Mid-Day	3	12 Dimensions		
Environment:	Forest, Desert, Snow	3	- Obviously a		
Weather:	Clear (+7nm), Haze (3-7nm), Low Ceiling/Visibility (<3000/3nn	n) <b>3</b>	large test		
Humidity:	Low (<30%), Medium (31-79%), High (>80%)	3	envelope		
Attack Azimuth:	Sun at back, Sun at beam, Sun on nose	3	how to search		
Attack Altitude:	Low (<5000'), High (>5000')	2			
Attack Airspeed:	Low (Mach .5), Medium (Mach .72), High (Mach .8)	3	IL ?		
JPADS Mode:	Autonomous, Laser Guidance	2			
	Combinations	139,968			



## Spanning the Battlespace – Traditional Test Designs







# Spanning the Battlespace - DOE













# **Efficiencies in Test - Fractions**







# We have a wide menu of design choices with DOE















Design Class	Pros	Cons		
Full Factorials	Easy to construct, analyze Robust to missing points	Get large fast with variables and levels		
Fractional Factorials	Smaller while spanning space	More fragile, may require extra runs to determine causes		
Response Surface	Moderate in size, more robust, model nonlinearities	Not many		
Optimal Designs	Very flexible for complex problems	Construct & analyze with care - more technical depth needed		
Space-Filling Designs	Excellent spanning properties	Difficulties in cause and effect linking		

 Simplified exposition: The best grad schools teach a 3-semester series in DOE

# Challenge 2: Which Points to Span the Relevant Battlespace?





- <u>Factorial</u> (crossed) designs let us *learn more* from the same number of assets
- We can also use Factorials to reduce assets while maintaining confidence and power
- Or we can *combine* the two

All four Designs share the same *power* and *confidence* 

How to support such an amazing claim?

		2 reps 2 vars			JP/	JPADS A			JPADS B		
		Ammo					2	2		2	
Food						2	2		2		
)											
		1 reps 3 vars			Z	 √	JPAC	S A	JPA	DS B	]
	Am			Amm	0		1			1	
		Egiin (Lo	JW)	W) Food			1		1		
	Nellis (High) A			Amm	no		1			1	
k			Food		1		1				
,	_	½ rep 4 va				Ļ	JPA	DS A	JPAD	SΒ	
			Ea	lin (Low	$_{/)}$ Ar	h	mo	-			
	Dawn (low light)	awn (low		(	'  Fc	00	d			1	
		Nellis (High		$h) \frac{Ar}{-}$	Ammo				1		
				$\frac{1}{ F_{C} }$	Food		1				
	Midday (bright)		Ealin (Low		$_{/)}$ Ar	Ammo				1	
		Midday			/ Fo		d				
		(bright)	ght)   <sub>Nell</sub>	llis (High)		Ammo					
					<sup>2</sup> /Fc	Food				1	

=> Switch to Excel File – JPADS Pancake.xls



# Equal Power? A preposterous claim ... how to justify it?



- Consider again our JPADS problem across 2 dimensions
- 13 wind speeds x 5 altitudes = 65 cases x 10 reps each = 650 trials
- Surely this will solve our problem with noise?

It will **not** ... we have 65 separate 10-sample trials





# Test as Science vs. Art: Experimental Design Test Process is Well-Defined



#### Planning: Factors Desirable and Nuisance

### Desired Factors and Responses

#### **Design Points**



#### **Test Matrix**



### Randomize & Block -> Results and Analysis

Effects ANOVA

Sum of

Sources

1.15

1.08

0.060

1.2245-003

CL.

D 🗃 🖬 🐰 🐚 🖻 🗿 ? 🍄

Evaluation

- 1 Cy (Analyzed) - 1 Croll (Analyzed

Cn (Analyzed)

CL (Analyzed

Namerical

Graphical

Analysis

### Model Build

#### Discovery, Understanding Prediction, Re-design







We understand operations, aero, mechanics, materials, physics, electromagnetics ...

To our good science, DOE adds the Science of Test



Bonus: Match faces to names - Ohm, Oppenheimer, Einstein, Maxwell, Pascal, Fisher, Kelvin



# It applies to <u>our</u> tests: DOE in 50+ operations over 20 years



- IR Sensor Predictions
- Ballistics 6 DOF Initial Conditions
- Wind Tunnel fuze characteristics
- Camouflaged Target JT&E (\$30M)
- AC-130 40/105mm gunfire CEP evals
- AMRAAM HWIL test facility validation
- 60+ ECM development + RWR tests
- GWEF Maverick sensor upgrades
- 30mm Ammo over-age LAT testing
- Contact lens plastic injection molding
- **30mm gun DU/HEI accuracy (A-10C)**
- GWEF ManPad Hit-point prediction
- AIM-9X Simulation Validation
- Link 16 and VHF/UHF/HF Comm tests
- TF radar flight control system gain opt
- New FCS software to cut C-17 PIO
- AIM-9X+JHMCS Tactics Development
- MAU 169/209 LGB fly-off and eval

- Characterizing Seek Eagle Ejector Racks
- SFW altimeter false alarm trouble-shoot
- TMD safety lanyard flight envelope
- Penetrator & reactive frag design
- F-15C/F-15E Suite 4 + Suite 5 OFPs
- PLAID Performance Characterization
- JDAM, LGB weapons accuracy testing
- Best Autonomous seeker algorithm
- SAM Validation versus Flight Test
- ECM development ground mounts (10's)
- AGM-130 Improved Data Link HF Test
- TPS A-G WiFi characterization
- MC/EC-130 flare decoy characterization
- SAM simulation validation vs. live-fly
  - Targeting Pod TLE estimates
- Chem CCA process characterization
- Medical Oxy Concentration T&E
  - Multi-MDS Link 16 and Rover video test

## Recap - Scientific Answers to Four Fundamental Test Challenges



Four Challenges faced by any test

- How many? A: sufficient samples to control our twin errors – false positives & negatives
- 2. Which Points? A: span/populate the battle-space while linking cause and effect with orthogonal run matrices
- 3. How Execute? A: Randomize and Block runs to exclude effects of the unknown-unknowns
- 4. What Conclusions? A: build math-models\* of input/output relations, quantifying noise, controlling error
- **DOE** effectively addresses all these challenges!



\* Many model choices: regression, ANOVA, mixed, Gen Lin Model, CART, Kriging, MARS
# Challenge 3: What Order? Guarding against "Unknown-Unknowns"



Randomizing <u>runs</u> protects from unknown background changes within an experimental period (due to Fisher)



## Blocks Protect Against Day-to-Day Variation





 Blocking <u>designs</u> protects from unknown background changes between experimental periods (also due to Fisher)





Sortie	Alt	Mach	MDS	Range	Tgt Aspect	OBA	Tgt Velocity	Target Type	Result
1	10K	0.7	F-16	4	0	0	0	truck	Hit
1	10K	0.9	F-16	7	180	0	0	bldg	Hit
2	20K	1.1	F-15	3	180	0	10	tank	Miss

 Graphical summary of performance, subject to P(hit)

- Change in scale
- Subset the domain to show desired trend
- Tell stories about performance  $\frac{1}{6.4}$
- Seldom quantify uncertainty
- Seldom test if result could be

By chance alone ...





## How Factorial Matrices Work -- a peek at the linear algebra under hood



### We set the X settings, observe Y

Simple 2-level, 2 X-factor design Where y is the grand mean, A,B are effects of variables alone and AB measures variables working together



Solve for b s.t. the error (e) is minimized

$$e = y - Xb$$
  

$$e'e = (y - Xb)'(y - Xb)$$
  

$$\frac{d(e'e)}{db} = \frac{d((y - Xb)'(y - Xb))}{db} = 0$$





$$\frac{d((\mathbf{y} - \mathbf{X}\mathbf{b})'(\mathbf{y} - \mathbf{X}\mathbf{b}))}{d\mathbf{b}} = \mathbf{0}$$

$$\frac{d((\mathbf{y} - \mathbf{X}\mathbf{b})'(\mathbf{y} - \mathbf{X}\mathbf{b}))}{d\mathbf{b}} = -2\mathbf{X}'(\mathbf{y} - \mathbf{X}\mathbf{b}) = \mathbf{0}$$

$$-2\mathbf{X}'(\mathbf{y} - \mathbf{X}\mathbf{b}) = \mathbf{0}$$

$$\mathbf{X}'\mathbf{y} - \mathbf{X}'\mathbf{X}\mathbf{b} = \mathbf{0}$$

$$\mathbf{X}'\mathbf{y} - \mathbf{X}'\mathbf{X}\mathbf{b} = \mathbf{0}$$

$$\mathbf{X}'\mathbf{X}\mathbf{b} = \mathbf{X}'\mathbf{y}$$

$$\mathbf{b} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y}$$

$$\mathbf{b} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y}$$

$$\mathbf{b} = \mathbf{0}$$

$$\mathbf{x}'\mathbf{x}\mathbf{b} = \mathbf{0}$$

$$\mathbf{x}'\mathbf{x}\mathbf{b} = \mathbf{0}$$





$$y = \beta_0 + \sum_i \beta_i x_i + \sum_i \beta_{ii} x_i^2 + \sum_{i \neq j} \beta_{ij} x_i x_j + \sum_i \beta_{iii} x_i^3 + \varepsilon \quad i = 1, 2, ..., k$$

- Very simple to fit models of the form above (among others) with polynomial terms and interactions
- Models fit with ANOVA or multiple regression software
- Models are easily interpretable in terms of the physics (magnitude and direction of effects)
- Models very suitable for "predict-confirm" challenges in regions of unexpected or very nonlinear behavior
- Run to run noise can be explicitly captured and examined for structure



## Analysis using DOE: CV-22 TF Flight





#### **DOE | S0-43**



## **Analysis Using DOE**



Gross		Turn			SCP	Pilot
Weight	SCP	Rate	Ride	Airspeed	Dev	Ratings
55	300.00	0.00	Medium	160.00	5.6	4.5
47.5	500.00	0.00	Medium	160.00	0.5	4.8
47.5	300.00	4.00	Medium	160.00	7.5	4.2
55	500.00	4.00	Medium	160.00	2.3	4.8
47.5	300.00	0.00	Hard	160.00	5.2	4.2
55	500.00	0.00	Hard	160.00	1.2	4.6
55	300.00	4.00	Hard	160.00	12.0	3.2
47.5	500.00	4.00	Hard	160.00	6.7	3.4
47.5	300.00	0.00	Medium	230.00	4.0	4.8
55	500.00	0.00	Medium	230.00	0.2	5.4
55	300.00	4.00	Medium	230.00	15.0	2.8
47.5	500.00	4.00	Medium	230.00	8.3	3.2
55	300.00	0.00	Hard	230.00	5.8	4.5
47.5	500.00	0.00	Hard	230.00	1.9	5.0
47.5	300.00	4.00	Hard	230.00	16.0	2.0
55	500.00	4.00	Hard	230.00	12.0	2.5
47.5	400.00	2.00	Medium	195.00	4.0	4.2
47.5	400.00	2.00	Hard	195.00	7.2	3.7
55	400.00	2.00	Medium	195.00	6.6	4.4
55	400.00	2.00	Hard	195.00	7.7	3.8



# **SCP Deviation Interpretation**





B: Turn Rate

# Pilot Ratings Response Surface





## **Radar Performance Results**



**SCP Deviation Estimating Equation** 

#### Prediction Model - Coded Units (Low=-1, High=+1)

=

#### Deviation from SCP

+6.51 -2.38 \* SCP +3.46 \* Turn Rate +1.08 \* Ride +1.39 \* Airspeed +0.61 \* Turn \* Ride +1.46 \* Turn \* Airspeed

Note magnitude and direction of effect s and what is not there – Gross Weight



## **Performance Predictions**



Name	Setting	Low Level	High Level
SCP	460.00	300.00	500.00
Turn Rate	2.80	0.00	4.00
Ride	Hard	Medium	Hard
Airspeed	180.00	160.00	230.00

	Prediction	95% PI low	95% PI high
Deviation from SCP	6.96	4.93	8.98
Pilot Ratings	3.62	3.34	3.90

Confirm or validate our model -- predict points that have not been tested and compare predictions to performance



# Actual Maverick H/K Test – A



## great success

- Extensive captive carry
  - 22 sorties
  - Approx 100 sim shots
  - Old/new seekers on each wing to equalize Wx
  - 3 platforms: F-16, F-15E, A-10
  - Eglin & Nellis
- Results approx 2x acq/trk range
- 9 shots comparable to current performance
- Full Disclosure Error Type III

Mission: N	MAV-1							
Eglin Rang	e Range Tin	ne: 0700-0900 (1	Dawn) Targe	t: Point (Tank)	Weather: As	Scheduled		
Launch Ai	rspeed: 400 KIA	S						
F-16 - #1	Left Wing:	Left Wing: CATM-65K on LAU-88Right Wing: TGM-65B on LAU-88						
Run#	Target Type	Altitude	Sun Angle	Missile Type	Cueing	Comments*		
1	Tank/Truck	18,000'	Sun at 6	H/K	Visual			
2	Tank/Truck	18,000'	Sun at 6	В	"			
3	Tank/Truck	1500'	Sun at 3/9	H/K	NAV/GPS			
4	Tank/Truck	1500'	Sun at 3/9	В	"			
5	Tank/Truck	1500'	Sun at 6	H/K	Radar			
6	Tank/Truck	1500'	Sun at 6	В	"			
7	Tank/Truck	18.000'	Sun at 3/9	H/K	LANTIRN			
8	Tank/Truck	Typica	al Mav H	/K F-16 F	Run Card			
F-16 - #2	Left Wing:	CATM-65K on	LA U-88	Right Wing: TG	M-65D on LAU	-88		
Run#	Target Type	Altitude	Sun Angle	Missile Type	Cueing	Comments*		
1	Tank/Truck	18,000'	Sun at 6	H/K	Visual			
2	Tank/Truck	18,000'	Sun at 6	D	"			
3	Tank/Truck	1500'	Sun at 3/9	H/K	NAV/GPS			
4	Tank/Truck	1500'	Sun at 3/9	D	"			
5	Tank/Truck	1500'	Sun at 6	H/K	Radar			
6	Tank/Truck	1500'	Sun at 6	D	"			
7	Tank/Truck	18,000'	Sun at 3/9	H/K	LANTIRN			
8	Tank/Truck	18,000'	Sun at 3/9	D	"			
* After sim	ulated pickle, si	mulate missile fl	yout by overfly	ving target and re	ecording seeker	video.		



## **The Basic Test Problem**





Answers to these questions determine your **strategy of experimentation**.

- Questions that must be answered for any test:
  - Which x's, z's should be changed, through what range, pattern?
  - How should the runs be ordered?
  - How many runs should we/can we make?
  - What method of analysis should be employed?
- Possible Objectives:
  - Characterizing where y's usually fall depending on x settings
  - Determining which variables have an influence on outputs
  - Determining where to set influential variables so outputs are near goal
  - Determining how to set inputs so variability of y is small
  - Determining where to set x's so that effects of z's are small

## Design of Experiments Test Process is Well-Defined

#### Planning: Factors Desirable and Nuisance

## Desired Factors and Responses

#### **Design Points**



#### **Test Matrix**



#### **Results and Analysis**

File Edit View Display O

Graph Col

Evaluation

- 1 Cy (Analyzed) - 1 Croll (Analyzed

Cn (Analyzed)

CL (Analyzed

Numerical

Graphical

Analysis

D## X 16 # ? \$

#### Model Build

#### **Discovery**, **Prediction**





## Caveat – we <u>need</u> good science!



We understand operations, aero, mechanics, materials, physics, electromagnetics ...

To our good science, DOE introduces the Science of Test



Bonus: Match faces to names - Ohm, Oppenheimer, Einstein, Maxwell, Pascal, Fisher, Kelvin





Consider how to characterize B-1B Radar Target Location Error as a

#### function of several factors.



■ +2 (DWWDLT, Rent-a-TIS)



## Pros and Cons of Various Test Strategies



Test Strategy	Description	Pros	Cons
DWWDLT	Do What We (They) Did Last Time	Conservative, preserves heritage	If not well thought-out, perpetuates mediocrity. No proof of goodness
"Rent A TIS"	Ask the Hardware Contractor	Good system understanding, good science in test. Track record.	As above, and no proof of goodness.
Subject Expertise/Intuition	Test Expert-Selected points	Expert assistance on where to test	Discourages new knowledge, unexpected behavior. Subjective, sparse coverage.
OFAT	Change one factor at a time	Know how changing one factor affects the system under test.	Ignores interactions (two factors change response). Sparse coverage of factor space.
Scenario/Cases	Use themes or war/use scenarios to pick test conditions	Good understanding of typical use performance.	Fails to answer why good-bad. Leads to "mythological tactics." Sparse coverage.
DOE	Decompose process into suspected cause-effect, replicate for power.	Most efficient and effective test strategy. Test becomes a science with rules.	Requires substantial training and experience, but can be taught and learned.

DOE – the only way we know to test broadly and deeply with power!

# B-1 OT Radar Mapping in One Mission (53d Wg)



**Problem**: Characterize B-1 radar coordinate accuracy for variety of operational setups.



**Results**: Similar accuracy across scan volume, target type, tail number.

**Design**: Responses: absolute error

Conditions: angle, side of nose, tail number, target, and range to target. 4 replicates.



**<u>Result:</u>** Single two-aircraft mission answered operational accuracy questions raised by 7 previous missions using conventional test methods.



# It applies to <u>our</u> tests: DOE in 36+ operations over 20 years



- IR Sensor Predictions
- Ballistics 6 DOF Initial Conditions
- Wind Tunnel fuze characteristics
- Camouflaged Target JT&E (\$30M)
- AC-130 40/105mm gunfire CEP evals
- AMRAAM HWIL test facility validation
- 60+ ECM development + RWR tests
- GWEF Maverick sensor upgrades
- 30mm Ammo over-age LAT testing
- Contact lens plastic injection molding
- 30mm gun DU/HEI accuracy (A-10C)
- GWEF ManPad Hit-point prediction
- AIM-9X Simulation Validation
- Link 16 and VHF/UHF/HF Comm tests
- TF radar flight control system gain opt
- New FCS software to cut C-17 PIO
- AIM-9X+JHMCS Tactics Development
- MAU 169/209 LGB fly-off and eval

- Characterizing Seek Eagle Ejector Racks
- SFW altimeter false alarm trouble-shoot
- TMD safety lanyard flight envelope
- Penetrator & reactive frag design
- F-15C/F-15E Suite 4 + Suite 5 OFPs
- PLAID Performance Characterization
- JDAM, LGB weapons accuracy testing
- Best Autonomous seeker algorithm
- SAM Validation versus Flight Test
- ECM development ground mounts (10's)
- AGM-130 Improved Data Link HF Test
- TPS A-G WiFi characterization
- MC/EC-130 flare decoy characterization
- SAM simulation validation vs. live-fly
  - Targeting Pod TLE estimates
- Chem CCA process characterization
- Medical Oxy Concentration T&E
- Multi-MDS Link 16 and Rover video test



## **Seven DOE Stories for T&E**





### We've selected these from 1000's to show T&E Transformation

## Testing to Diverse Requirements: SDB II Shot Design







Test Objective:

- SPO requests help 46 shots right N?
- Power analysis what can we learn?
- Consider Integrated Test with AFOTEC
- What are the variables? We do not know yet ...
- How can we plan?
- What "management reserve"

DOE Approach:

- Partition performance questions: Pacq/Rel + laser + coords + "normal mode"
- Consider total test pgm: HWIL+Captive+Live
- Build 3x custom, "rightsize" designs to meet objectives/risks

🕌 Power vs. Actual value (p) 📃 🗖 🔀
Help ← Perf shift
46 shots too few to 7- Check binary 9- Values +/- 15-20% 5- Coa 5 55 5 5 5 7 75 5 5 55
Vertical (y) axis Power   Horizontal (y) axis Actual value (p)   from 50 to 85 by 01  Persistent Show Data Redraw Close

#### Results:

			Performance Shift from KPP in Units of 1 Standard Deviation						
-	Binary B	Shots	0.25	0.5	0.75	1	1.25	1.5	2
	Dillary P <sub>aca</sub>	4	0.176	0.387	0.65	0.855	0.958	0.992	0.999
		6	0.219	0.52	0.815	0.959	0.995	0.999	0.999
	N=200+	8	0.259	0.628	0.905	0.989	0.999	0.999	0.999
		10	0.298	0.714	0.952	0.997	0.999	0.999	
_	Domo locar	12	0.335	0.783	0.977	0.999	0.999	0.999	
	Demo laser	14	0.371	0.837	0.989	0.999	0.999	0.999	
		16	0.406	0.878	0.994	0.999	0.999		
	+ coords	18	0.44	0.909	0.997	0.999	0.999		
		20	0.472	0.933	0.998	0.999	0.999		
	$N = 1 \Delta 2$	24	0.532	0.964	0.999	0.999			
		28	0.587	0.981	0.999	0.999			
		32	0.636	0.99	0.999	0.999			
	Prove	36	0.681	0.995	0.999				
	11010	40	0.721	0.997	0.999				
	normal	50	0.802	0.999	0.999	32-	shot fa	actorial	
	normai	60	0.862	0.999		6	croone	a /1-8	
		70	0.904	0.999				54-0	
	mode N=32	80	0.934	0.999		varia	ibles to	o 0.5 si	td
		100	0.97	0.999		dev	shift fre	om KP	Р
							orment	5	Ż

Integrate 20 AFOTEC shots for "Mgt Reserve"



## Acquisition: F-15E Strike Eagle Suite 4E+ (circa 2001-02)



	<ul> <li>Test Objectives:</li> <li>Qualify new OFP Suite for Strikes with new radar modes, smart weapons, link 16, etc.</li> <li>Test must address dumb weapons, smart weapons, comm, sensors, nav, air-to-air, CAS, Interdiction, Strike, ferry, refueling</li> <li>Suite 3 test required 600+ sorties</li> </ul>
<ul> <li>OE Approach:</li> <li>Build multiple designs spanning:</li> <li>EW and survivability</li> <li>BVR and WVR air to air engagements</li> <li>Smart weapons captive and live</li> <li>Dumb weapons regression</li> <li>Sensor performance (SAR and TP)</li> </ul>	<ul> <li>Results:</li> <li>Vast majority of capabilities passed</li> <li>Wrung out sensors and weapons deliveries</li> <li>Dramatic reductions in usual trials while spanning many more test points</li> <li>Moderate success with teaming with Boeing on design points (maturing)</li> </ul>

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## Strike Weapons Delivery a Scenario Design Improved with DOE

	<b>Cases Design</b>	Same N -	-50% N	Comparison
		Factorial	Factorial	
Cases	6	32	16	2.5 to 5x more (530%)
n	10	2	2	
Ν	60	64	32	-50% to +6.7% more
Sensitivity $(\delta/\sigma)$	1	1	1	
α	5%	5%	5%	Same
β	20%	2.5%	20%	1/10 <sup>th</sup> error rate
<b>Power</b> (1-β)	80%	97.50%	80%	detect shifts equal or





# Case: Secure SATCOM for F-15E Strike Eagle



	<ul> <li>Test Objective:</li> <li>To achieve secure A-G comms in Iraq and Afghanistan, install ARC- 210 in fighters</li> <li>Characterize P(comms) across geometry, range, freq, radios, bands, modes</li> <li>Other ARC-210 fighter installs show problems – caution needed here!</li> </ul>			
DOE Approach:	Results:			
Use Embedded Face-Centered CCD design (created for X-31 project, last slide)	For higher-power radio – all good			
Gives 5-levels of geometric variables across radios & modes	For lower power radio, range problems			
• Speak 5 randomly-generated words and score number correct	Despite urgent timeframe and			
• Each Xmit/Rcv a test event – 4 missions	canceled missions, enough proof to field			

Source: F-15E Secure SATCOM Test, Ms. Cynthia Zessin, Gregory Hutto, 2007 F-15 OFP CTF 53d Wing / 46 Test Wing, Eglin AFB, Florida

# Case: GWEF Large Aircraft IR Hit Point Prediction



#### **DOE Approach**:

- Aspect 0-180 degees, 7each
- Elevation Lo,Mid,Hi, 3 each
- Profiles Takeoff, Landing, 2 each
- Altitudes 800, 1200, 2 each
- Including threat 588 cases
- With usual reps nearly 10,000 runs
- DOE controls replication to min needed



**Test Objective:** 

- IR man-portable SAMs pose threat to large aircraft in current AOR
- Dept Homeland Security desired Hit point prediction for a range of threats needed to assess vulnerabilities
- Solution was HWIL study at GWEF (ongoing)

#### **Results**:

- Revealed unexpected hit point behavior
- Process highly interactive (rare 4-way)
- Process quite nonlinear w/ 3<sup>rd</sup> order curves
- Reduced runs required 80% over past
- Possible reduction of another order of magnitude to 500-800 runs

#### **Case: Reduce F-16 Ventral Fin Fatigue from Targeting Pod Face-Centered CCD** max test altitude 15 Embedded F-CCD 0.7 Expert Chose 162 test points Ventral fin 0.4 0.5 0.6 **DOE Approach**: **Results**: Many alternate designs for this 5-dimensional

space ( $\alpha$ ,  $\beta$ , Mach, alt, Jets on/off)

		1	Percent	
		Test	of	
Choice	Design Name	Points	Baseline	Model
Base	Subject-expert	324	100%	none - inspection
1	CCD	58	18%	quadratic + interactions
2	FCD	58	18%	quadratic + interactions
3	Fractional FCD	38	12%	quadratic + interactions
4	1/3rd fraction 3-level	54	17%	quadratic interactions
5	Box-Behnken	54	17%	quadratic + interactions
6	S-L Embedded FCD	76	23%	Up to cubic model
	Choice           Base           1           2           3           4           5           6	ChoiceDesign NameBaseSubject-expert1CCD2FCD3Fractional FCD41/3rd fraction 3-level5Box-Behnken6S-L Embedded FCD	ChoiceDesign NameTestBaseSubject-expert3241CCD582FCD583Fractional FCD3841/3rd fraction 3-level545Box-Behnken546S-L Embedded FCD76	ChoiceDesign NameTestofBaseSubject-expert324100%1CCD5818%2FCD5818%3Fractional FCD3812%41/3rd fraction 3-level5417%5Box-Behnken5417%6S-L Embedded FCD7623%

- New design invented circa 2005 capable of efficient flight envelope search
- Suitable for loads, flutter, integration, acoustic, vibration full range of flight test
- Experimental designs can increase knowledge while dramatically decreasing required runs
- A full DOE toolbox enables more flexible testing

# Case: CFD for NASA CEV



Interaction

D: TipShape

C: TipFineRatio





# A Strategy to be the *Best* ... Using Design of Experiments



- Inform OT Leadership of Statistical Thinking for Test
- Adopt most powerful test strategy (DOE)
- Train & mentor total Ops Test teams
- Combo of AFIT, Center, & University
- Revise AF T&E policy, procedures
- Share these test improvements <u>Adopting DOE</u> <u>Targets</u>
  - 53d Wing & AFOTEC
  - 18 FTS (AFSOC)
    RAF AWC
- \_\_\_\_ ASC & ESC

HQ AFMC

Service DT&E

- DoD OTA: DOT&E, AFOTEC, ATEC,
- OPTEVFOR & MCOTEA
- AFFTC & TPS
- 46 TW & AAC
- AEDC





# Five Steps to Teach Testers to Fish...





more skilled at creating leaders." -- Dr. John Kotter



### From 53d Wing Test Manager's Handbook\*:

"While this [*list of test strategies*] is not an allinclusive list, these are well suited to operational testing. The test design policy in the 53d Wing supplement to AFI 99-103 mandates that we achieve confidence and power across a broad range of combat conditions. After a thorough examination of alternatives, the DOE methodology using factorial designs should be used whenever possible to meet the intent of this policy."

# March 2009: OTA Commanders Endorse DOE for both OT & DT



"Experimental design further provides a valuable tool to identify and mitigate risk in all test activities. It offers a framework from which test agencies may make wellinformed decisions on resource allocation and scope of testing required for an adequate test. A DOE-based test approach will not necessarily reduce the scope of resources for adequate testing.

Successful use of DOE will require a cadre of personnel within each OTA organization with the professional knowledge and expertise in applying these methodologies to military test activities. Utilizing the discipline of DOE in all phases of program testing from initial developmental efforts through initial and follow-on operational test endeavors affords the opportunity for rigorous systematic improvement in test processes."



# Nov 2008: AAC Endorses DOE for RDT&E Systems Engineering



AAC Standard Systems Engineering Processes and Practices

# July 2009: 46 TW Adopts DOE as default method of test

6TW DOE policy	. pdf - Adobe Reader
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	DEPARTMENT OF THE AIR FORCE HEADQUARTERS 48 <sup>th</sup> TEST WING (AFMC) 101 WEST D AVE SUITE 226 EGLIN AIR FORCE BASE FLORIDA 32542-5000
	7 Jul 09
	POLICY LETTER FOR ALL 46 TW PERSONNEL
	FROM: 46 TW/CC
	SUBJECT: Design of Experiments (DOE) is 46 TW Primary Test Strategy
	1. Under AFSO21, our Chief challenged the Air Force Test and Evaluation (T&E) Enterprise to make T&E more effective and efficient. For the past several years, we've monitored our sister test organizations as they applied the principles of DOE as their primary test strategy. During 2007-09, we engaged in a robust "DOE proof of concept" phase spanning more than 40 projects throughout our test portfolio. Trials are concluded; DOE works! We can improve 46 TW tests by adopting the principles of the science of test in every program where it makes sense.
	2. Therefore, each Test Squadron will use DOE in all their testing when they have control of test design and when the number of test events consists of more than a mere demonstration. Exceptions will be approved by the appropriate Group Commander.
	3. All 46 TW-designed test plans will 1) mathematically cite the statistical risks implied by their proposed test program, and 2) achieve high confidence and power over a broad test volume. Suitable modifications to this policy will be made for software tests. Policy compliance at the Group (or squadron level where appropriate) will be tracked quarterly at Wing Staff meetings using the metrics in attachment 1. The office of the Wing Operations Analyst is the primary technical point of contact for this policy.



# We Train the Total Test Team ... but first, our Leaders!



### Leadership Series

- **DOE Orientation (1 hour)**
- ∑ **DOE for Leaders** (half day)
- ∑ Introduction to Designed Experiments (PMs- 2 days)

**OA/TE** Practitioner Series

- 10 sessions and 1 week each
- Reading--Lecture--Seatwork
- Basic Statistics Review (1 week)
  - Random Variables and Distributions
  - Descriptive & Inferential Statistics
  - Thorough treatment of t Test
- Applied DOE I and II (1 week each)
  - Advanced Undergraduate treatment
  - Graduates know both how and why

► Journeymen Testers


# **Continuation Training**



- Weekly seminars online
- Topics wide ranging
  - New methods
  - New applications
  - Problem decomposition
  - Analysis challenges
  - Reviewing the basics
  - Case studies
  - Advanced techniques
- DoD web conferencing
- Q&A session following

#### Operations Analyst Forum/DOE Continuation Training for 04 May 09:

Location/Date/Time: B1, CR220, Monday, 04 May 09, 1400-1500 (CST) Purpose: OPS ANALYST FORUM, DOE CONTINUATION TRAINING, USAF T&E COLLABORATION

Live: Defense Connect Online: https://connect.dco.dod.mil/eglindoe

Dial-In: (VoIP not available yet) 850-882-6003/DSN 872-6003

Data:

- USAF DOE CoP
- <u>https://afkm.wpafb.af.mil/SiteConsentBanner.aspx?ReturnUrl=%2fASPs%2fCoP%2fOpenCoP.asp%3fFilter%3dOO-TE-MC-79&Filter=OO-TE-MC-79</u> (please let me know if this link works for you)

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## **Our Goal**











#### John Kotter's Recipe for Change and Institutionalization 1 Create a sense of urgency Sculpt and Polish a Vision (and credible path to achieve) 2 3 Assemble a *Powerful* Coalition 4 Over-Communicate Vision x10 x100! Empower People (ID, direct, permit, train & equip) 5 Get the *quick, core* wins (projects) 6 Do **not** declare victory & retire early 8 Anchor it: Change systems, organization & People -- from *Leading Change*





- Gain AAC Commander endorsement and policy announcement
- ✓ Train and align leadership to support initiative
- Commence training technical testers
- ✓ Launch multiple quick-win pilot projects to show applicability
- Communicate the change at every opportunity
- ✓ Gain AAC leadership endorsement and align client SPOs
- Influence hardware contractors with demonstrations and suitable contract language
- Keep pushing the wheel to build momentum
- Confront nay-sayers and murmurers
- Institutionalize with promotions, policies, Wing structures and practices
- Roll out to USAF at large and our Army & Navy brethren

# **But Why Should** *T&E* **Pursue DOE?**

- Why:
  - It's the scientific, structured, objective way to build better ops tests
  - DOE is faster, less expensive, and more informative than alternative methods
  - Uniquely answers deep and broad challenge: Confidence & Power across a broad battlespace
  - Our less-experienced testers can reliably succeed
  - Better chance of getting it right!

### What I Need ...

- Practitioners students!
- People a field grade civilian ea Sqdn
- Projects give me the biggest and baddest
- Accountability "if not DOE, why not??"

"To call in the statistician after the experiment is ... asking him to perform a postmortem examination: he may be able to say what the experiment died of." Address to Indian Statistical Congress, 1938.







What's Your Method of Test?



# **DOE: The Science of Test**



## **Questions**?