



Modeling and Simulation for Guided Mortar Projectiles

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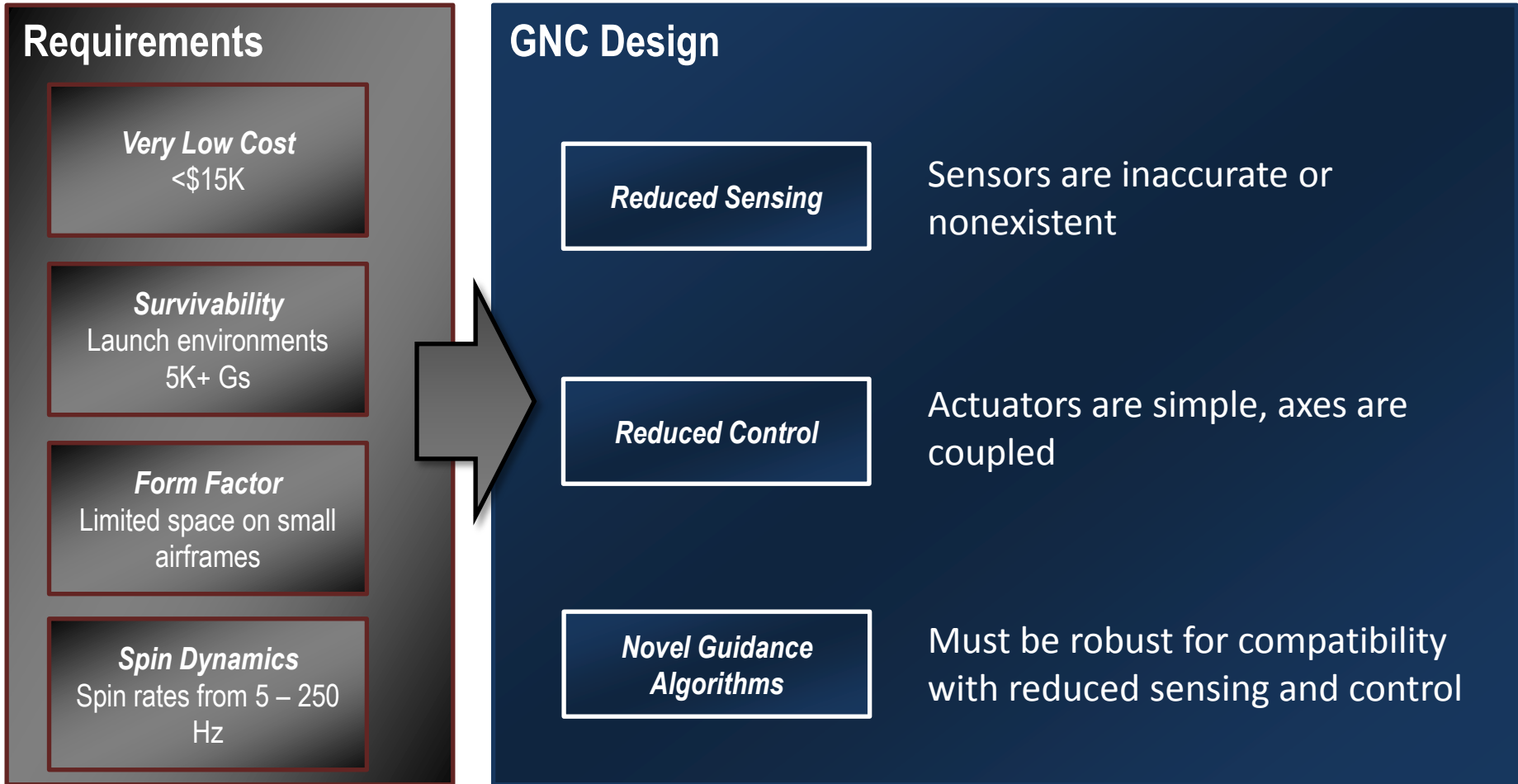
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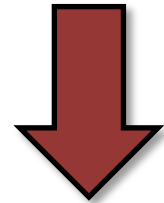
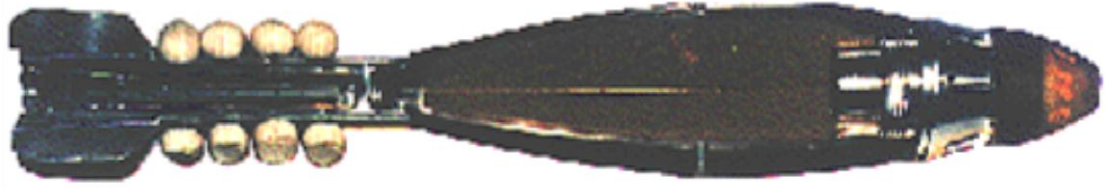
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Projectile GNC



High fidelity modeling and simulation is critical for the success of guided projectiles!

GNC Design - 60mm Guided Mortar



Larger fins for lift, stability, and roll

Standard Mortar Body

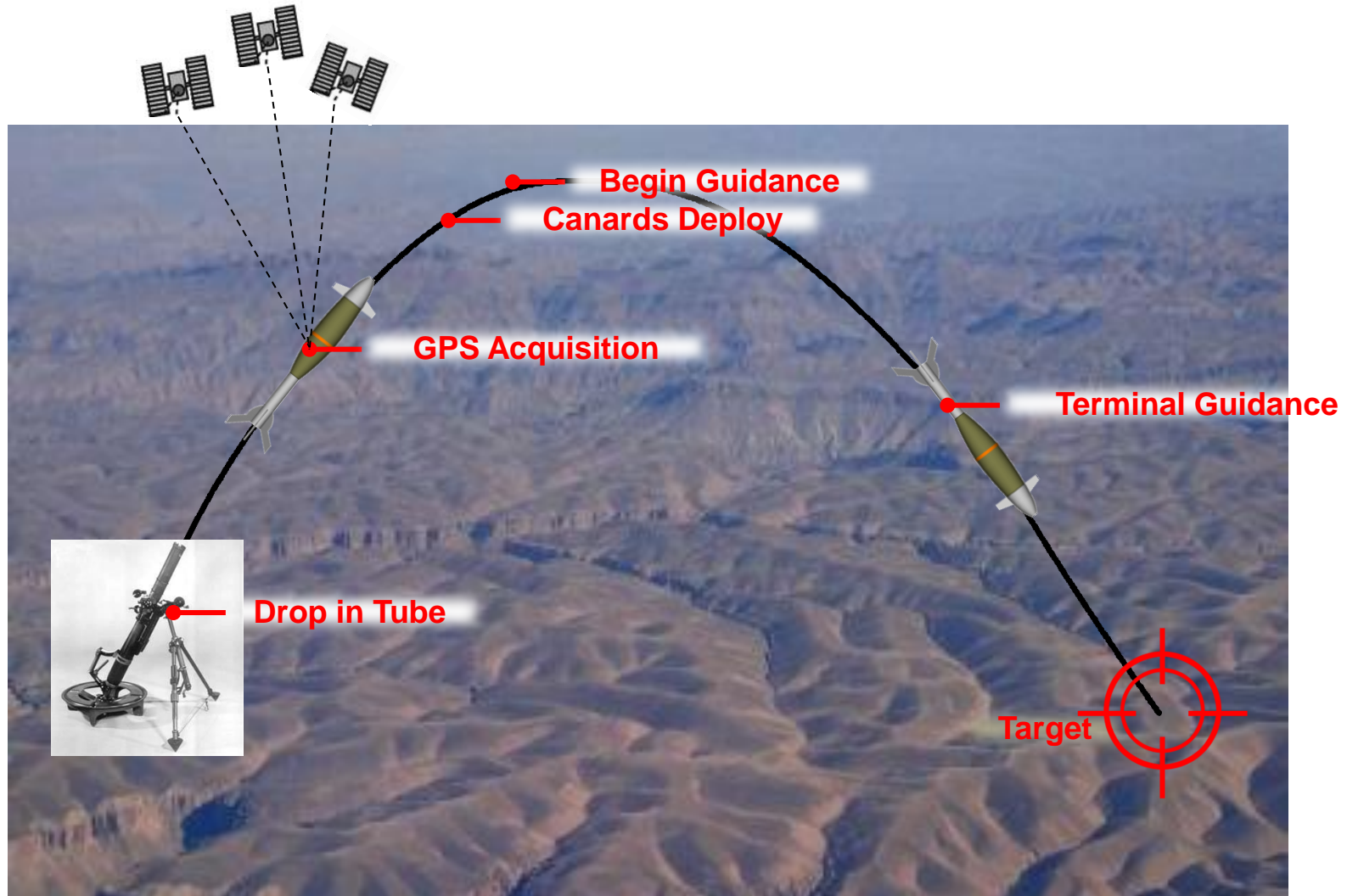
Extended Ogive for GNC Components

Reduced Control

Canards with Limited Actuation

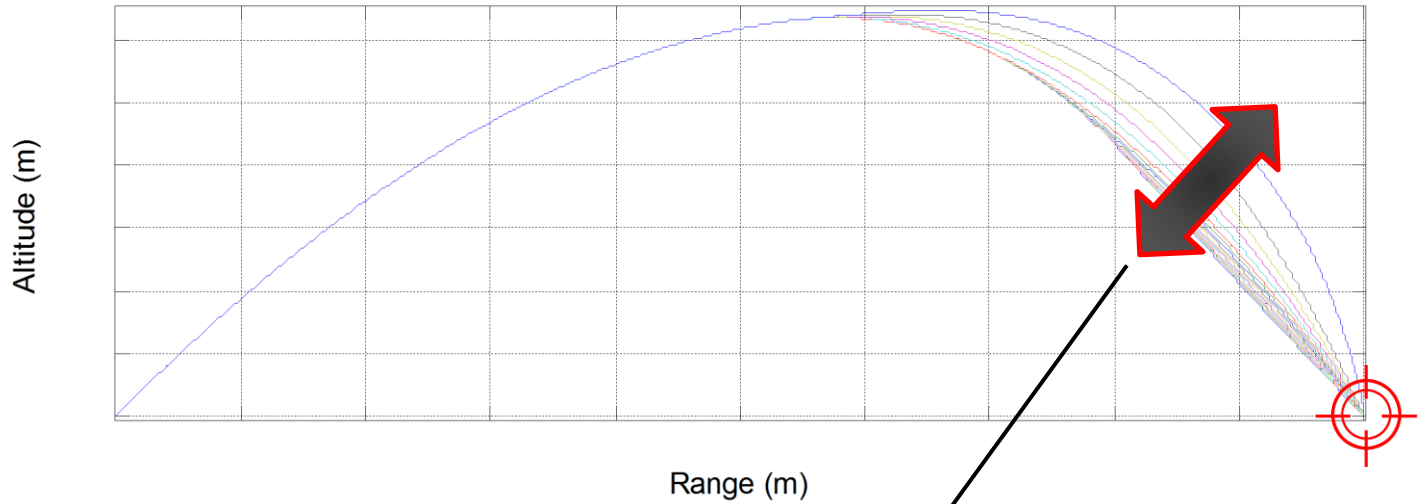
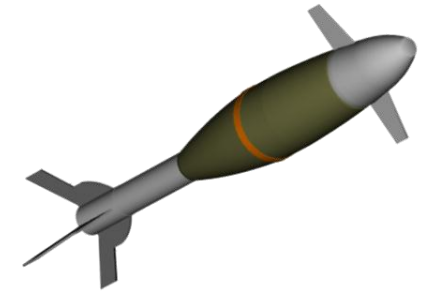
Reduced Sensing

GPS-Only w/ Roll Angle Output



Novel Guidance

- Guidance algorithm must take advantage of ballistic trajectory
- Do not want to fight gravity
- Additional trajectory shaping can improve angle of fall



Novel Guidance Algorithms

**Gravity Compensation/
Trajectory Shaping**

Aerodynamic Model

Direct Table Lookup Coefficients

- Extremely versatile – capture any asymmetries and nonlinearities
- Wind tunnel / CFD compatible format
- High angle of attack

$$F_z = \bar{q}A \left(C_z + \frac{pd}{2V} C_{zp} + \frac{qd}{2V} C_{zq} \right)$$

$$m = \bar{q}Ad \left(C_m + \frac{pd}{2V} C_{mp} + \frac{qd}{2V} C_{mq} \right)$$

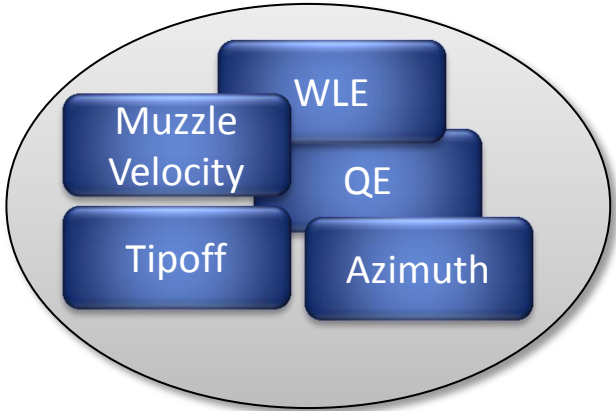
Polynomial Approximations

- Physics-based simplifications
- Spark range / aero predictor compatible format
- Flight test data reduction parameter fits

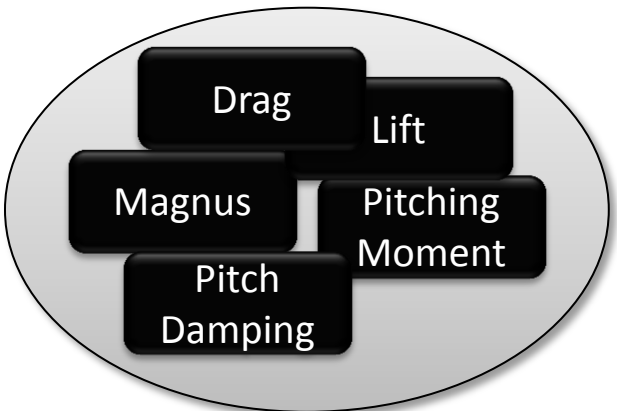
$$F_z = \bar{q}A \left(- \left[C_{N\alpha} + C_{N\alpha 3} \sin^2 \bar{\alpha} \right] \frac{w}{V} - \frac{pd}{2V} C_{Yp\alpha} \frac{v}{V} + \frac{qd}{2V} C_{Nq} \right)$$

$$m = \bar{q}Ad \left(\left[C_{m\alpha} + C_{m\alpha 3} \sin^2 \bar{\alpha} \right] \frac{w}{V} + \frac{pd}{2V} C_{np\alpha} \frac{v}{V} + \frac{qd}{2V} C_{mq} \right)$$

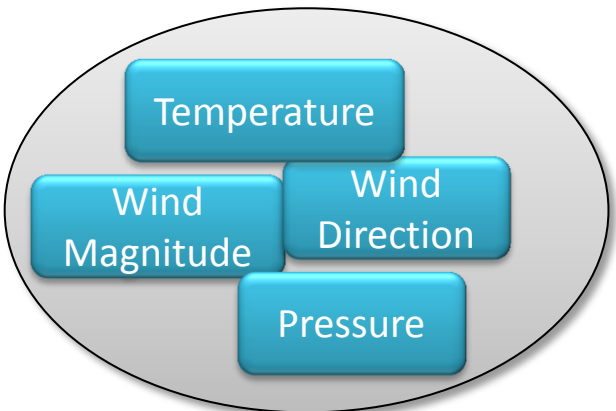
Error Budget



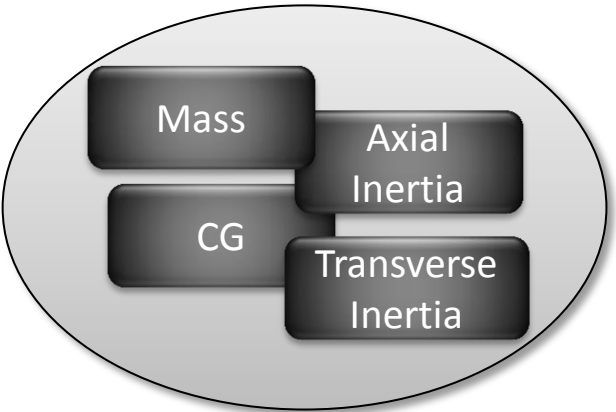
Body States



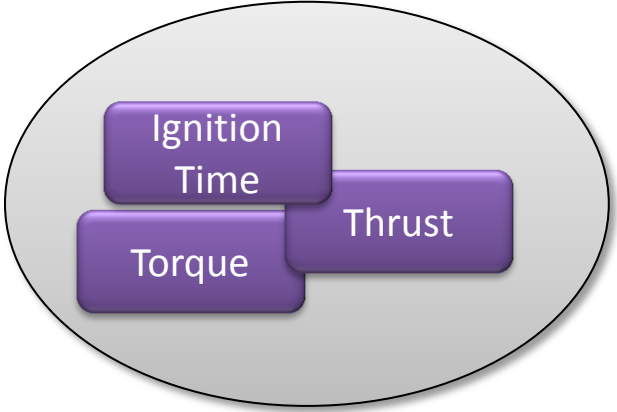
Aerodynamics



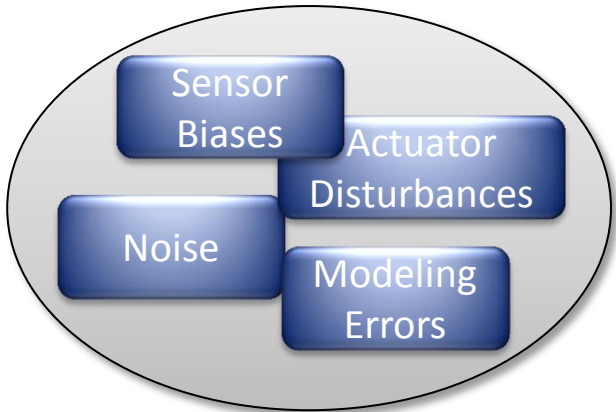
Environment



Mass Properties



Rocket Motor

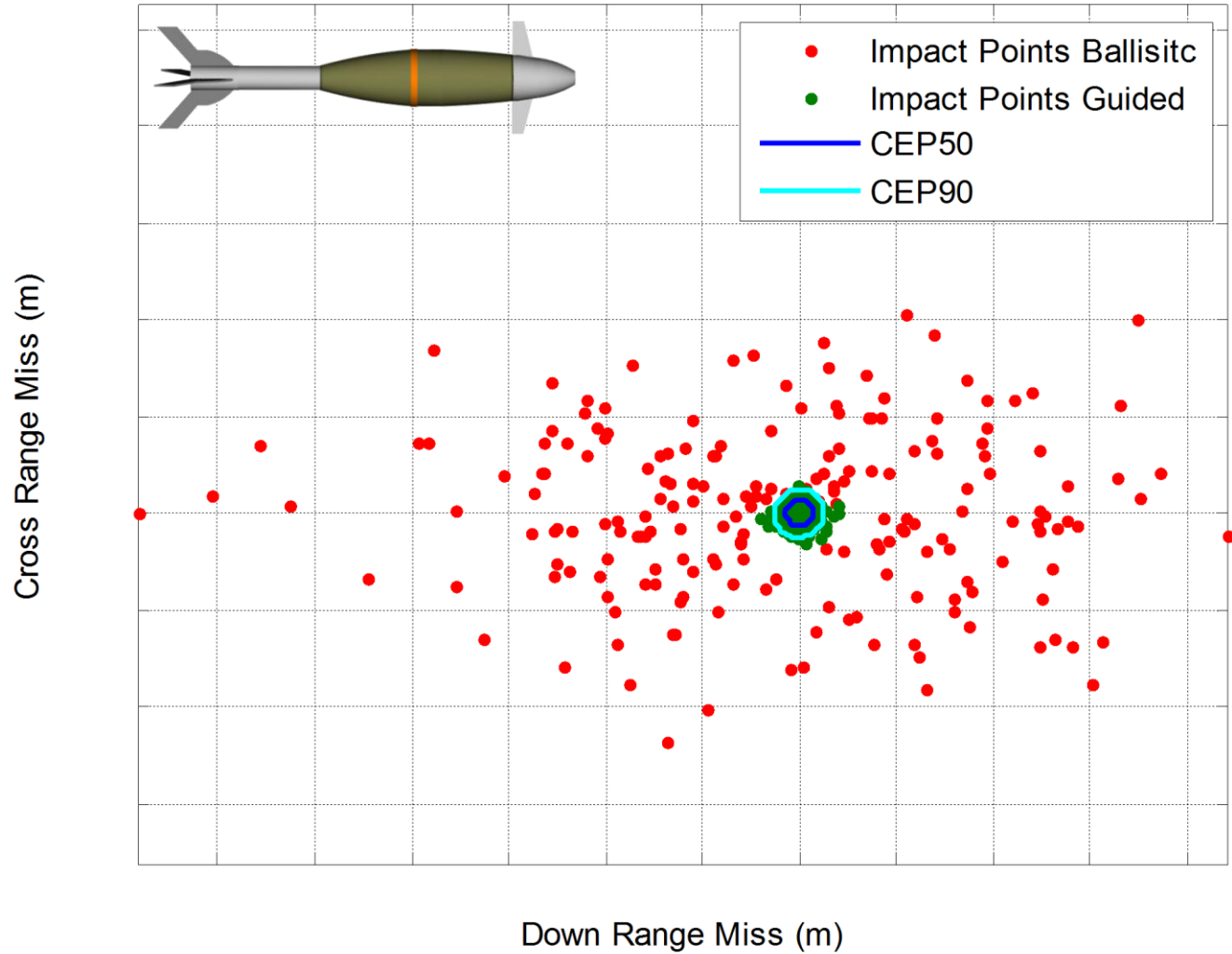


GNC

- **3 Types: Mission-to-Mission, Weapon-to-Weapon, Round-to-Round**

Accuracy Results

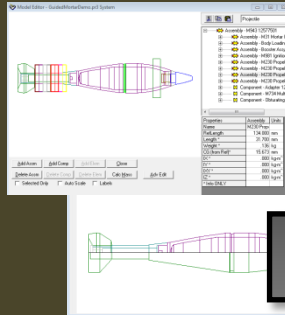
- Monte Carlo trials based on error budget
- CEP50 vs. CEP90
- Randomizing
 - Missions
 - Weapons
 - Rounds



PRODAS Environment

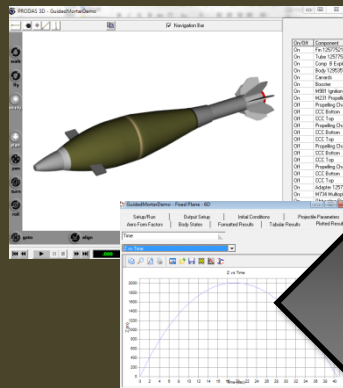
Modeling

- Projectile Modeler
- Aero Prediction
- Mass Properties
- Rocket Motor
- Initial Conditions
- Error Budgets
- MET

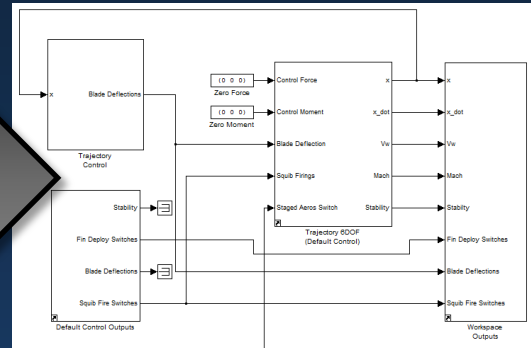


Visualization

- 3D Animations
- Extensive Plotting



MATLAB/Simulink Environment



Development

- Leverage All MATLAB/Simulink Toolboxes and Blocksets
- Focused Effort on GNC Design

Simulation

- Validated 6+DOF Trajectory Engine
- Seamless Data Interface and Execution Between PRODAS and MATLAB

Product Tests

Hardware-In-the-Loop (HIL)

- Use the same simulation to drive the HIL fixture



Embedded Code Generation

- Automatically generate flight code from the Simulink model



Fire Control

- Simulation software is the basis of fire control software

