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## **Extraction of Aerodynamic Coefficients via Data Fusion**

Alan Hathaway

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Arrow Tech Associates, Inc.

- Problem Statement
- Solution
- Details
- Summary & Conclusions

- **How does engineer make best use of all available aerodynamic data?**
- **Background:**
  - **Multiple Instrumentation Sources Available to Extract Aerodynamics**
    - **Ground-Based Instrumentation**
      - Doppler Radar(s)
      - Position Radar
      - KTM Optical Camera Trackers
    - **On-Board Instrumentation**
      - GPS
      - Accelerometers
      - Sun Sensors
- **Instrumentation sources may cover only part of the flight**
- **Instrumentation may suffer signal drop-out & reacquisition of signal**
- **ANSWER: Data Fusion via Parameter Identification**

***Extraction of Aero Coefficients is Most Accurate Using Parameter Identification***

- **Assume:** System Model has unknown parameters influencing flight
  - Guided or Ballistic Flight
- **Goal:** Determine magnitude of unknown parameters to obtain simultaneous best fit all of the observed data
  - Flight Simulation with “End Model” matches observed flight path and dynamic motion with minimum errors
  - Compare predicted flight motion using standard Equations of Motion with measured motion, differentially adjust aerodynamics to minimize differences

***Parameter Identification Provides Most Accurate  
Assessment from Largest Portions of Data***

- **Start:** Standard Equations of Motion, Estimates of Initial Conditions & Aerodynamics
- Partial Differentiation for each coefficient to generate parametric equations
- Numerically integrate to obtain partial derivatives for each coefficient
- Differential correction equation from Taylor Expansion
- Solve for aerodynamics & look at residuals, plug solutions into Equations of motion & iterate until change in residuals is “zero”

***Parameter Identification uses standard Equations of Motion to generate sensitivity matrix; most sensitive parameters fit first***

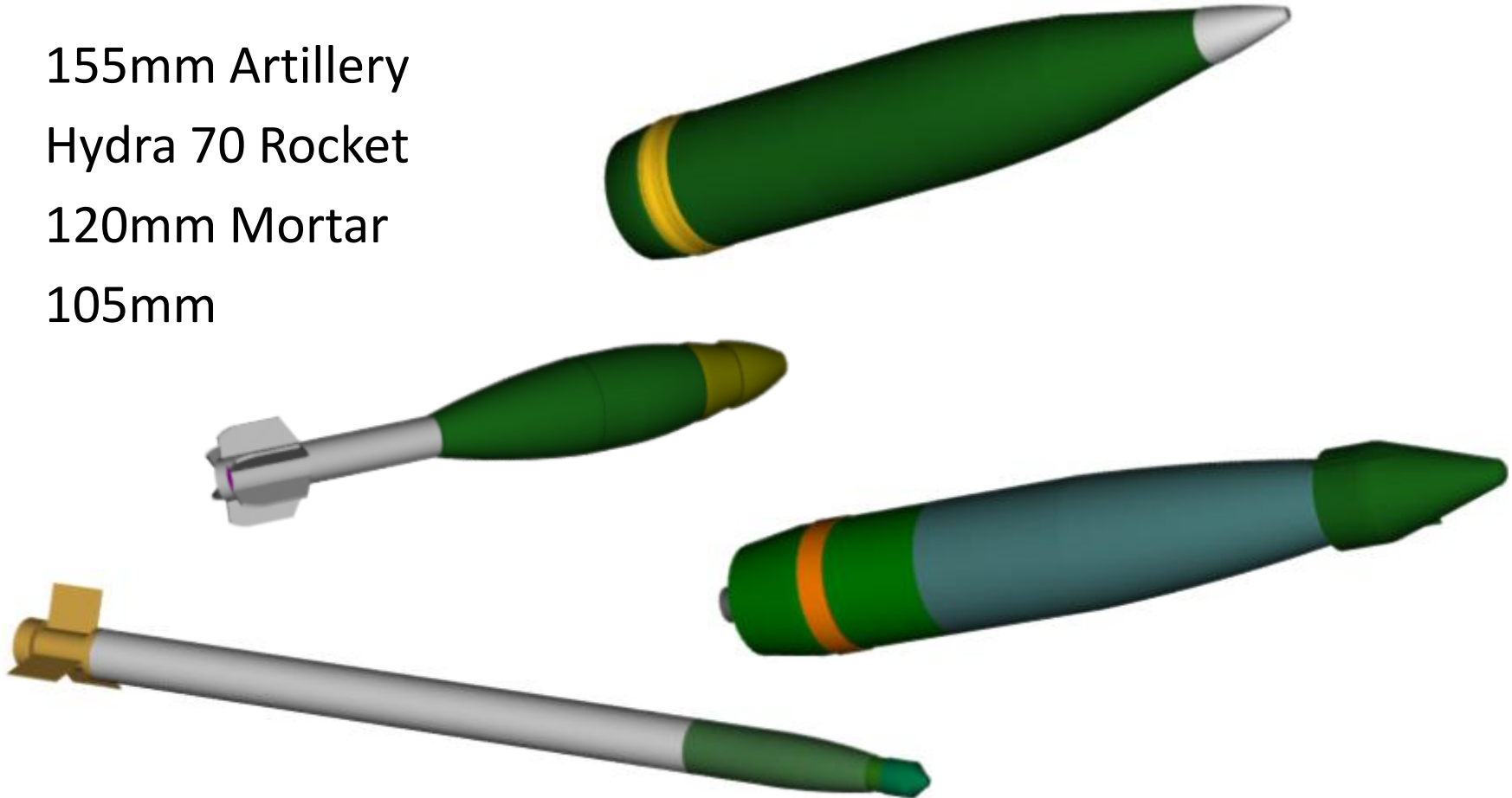
- **On-Board Sensors & Ground Based Doppler Radar**
  - Radar Modified 4DoF
  - Linear Theory
  - 4 DoF Angular & Swerve Motion Analysis
  - 6 DoF Fixed Plane
  - Body Fixed 6 DoF with Control Forces & Moments
  - GPS Data
- **Ground Based Doppler Radar and KTM Optical Tracker**
  - Sectional Trajectory Reconstruction
  - Radar Modified 4 DoF
  - GPS Data

***Data Fusion Works with a Variety of  
Instrumentation & Sensors***

- Data Screening (e.g. does data have large noise?)
- Estimates of Initial Velocity & Conditions (Gun QE & Az)
- Estimates of Burn-on & Burn-out times
- Overlapping 4 DoF sectional fits of complete trajectory via Equations of Motion
- Axial Force & Roll vs. Time & Mach and/or Thrust vs. Time
- Added screening for Erroneous Data based on simulations
- Complete multi-parameter 6DoF Simulations w/ Control Forces (w/ On-board sensors only)

***Screen, fit, screen, fit.... Until errors are minimized,  
Applicable to ballistic & guided projectiles***

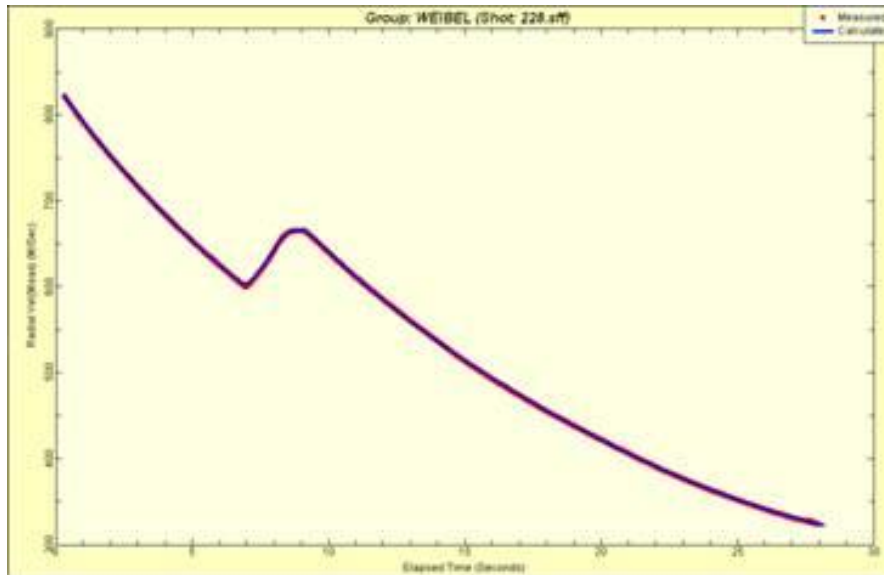
- 155mm Artillery
- Hydra 70 Rocket
- 120mm Mortar
- 105mm



***Wide range of projectiles & uses;  
Ballistic, Powered & Guided***



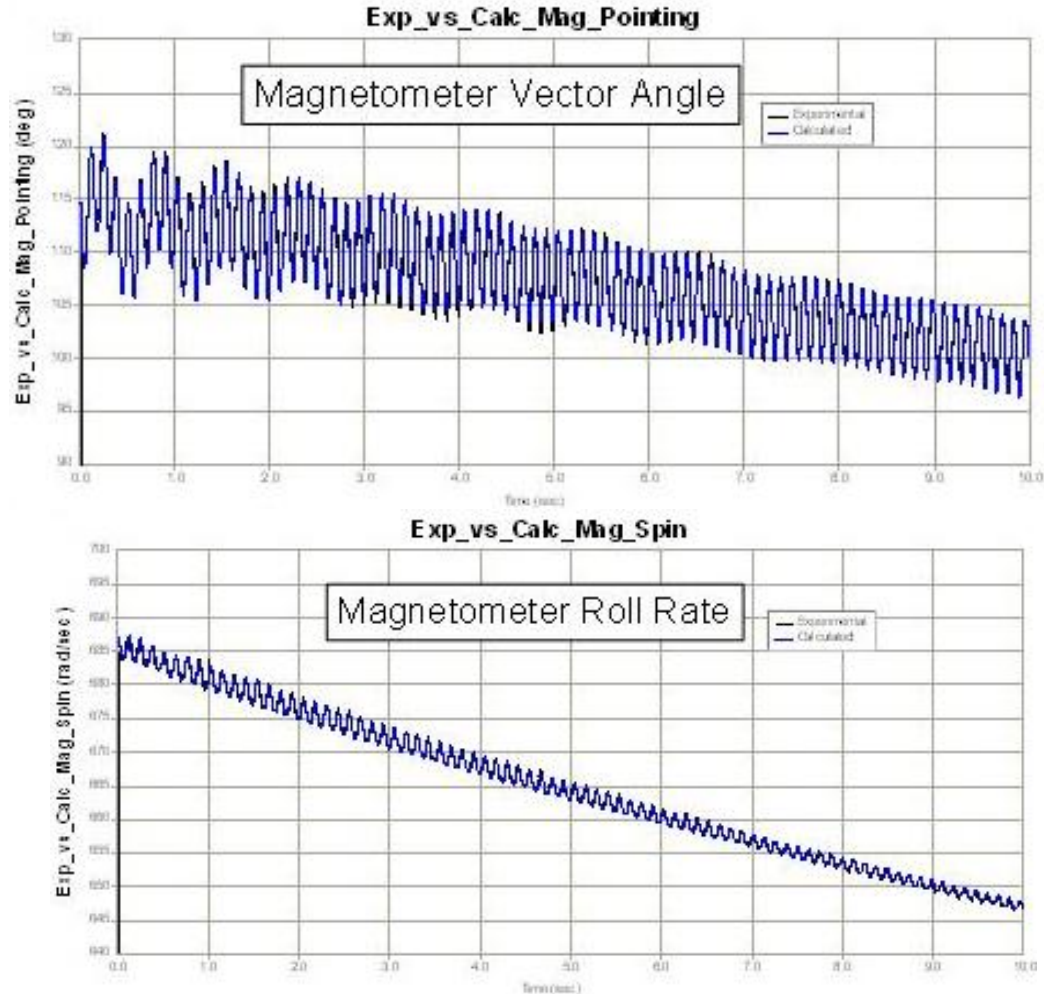
- Position & Velocity Radars
- “Behind the gun” & “Down Range” Doppler
- Position radar provides range, Az & El Data
- Tracking Doppler provides velocity, Az & El data



Radial Velocity vs Time  
Fit Error 0.62 meters/sec

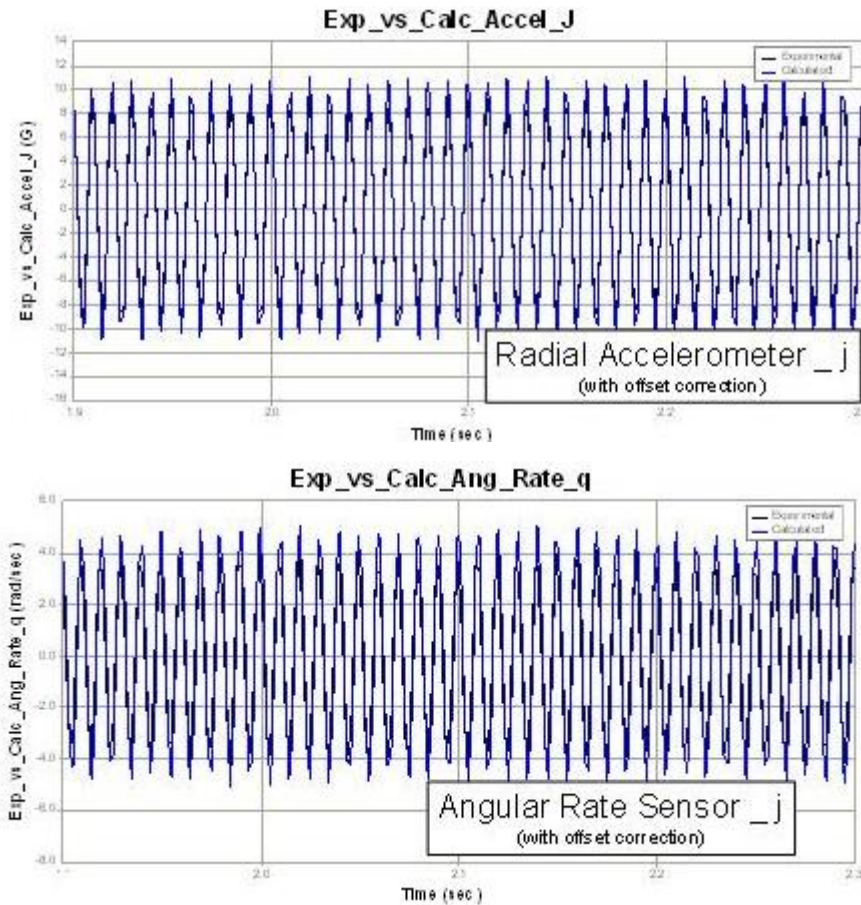
***Velocity-time data basis for drag/thrust solution***

# Magnetometer Measured vs. Fit



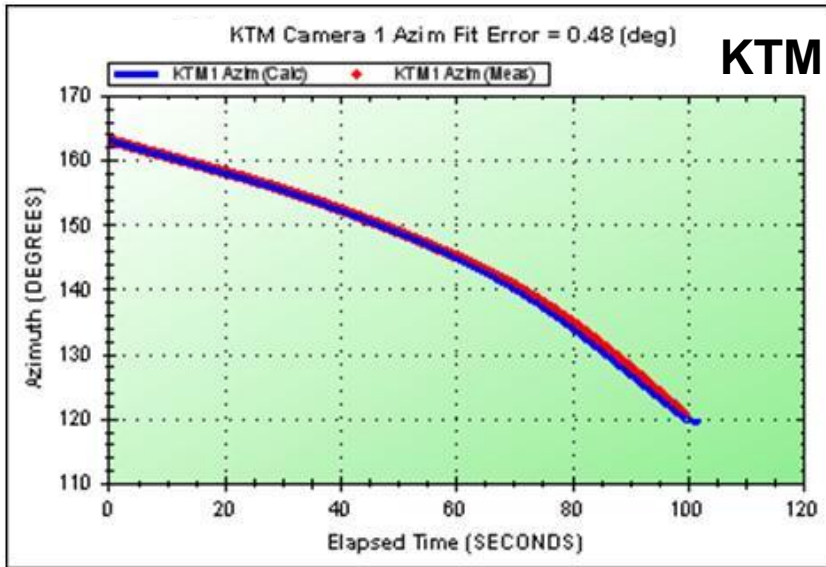
***Magnetometer Provides Yaw & Roll Angle Data***

# Angular Accelerations & Rates

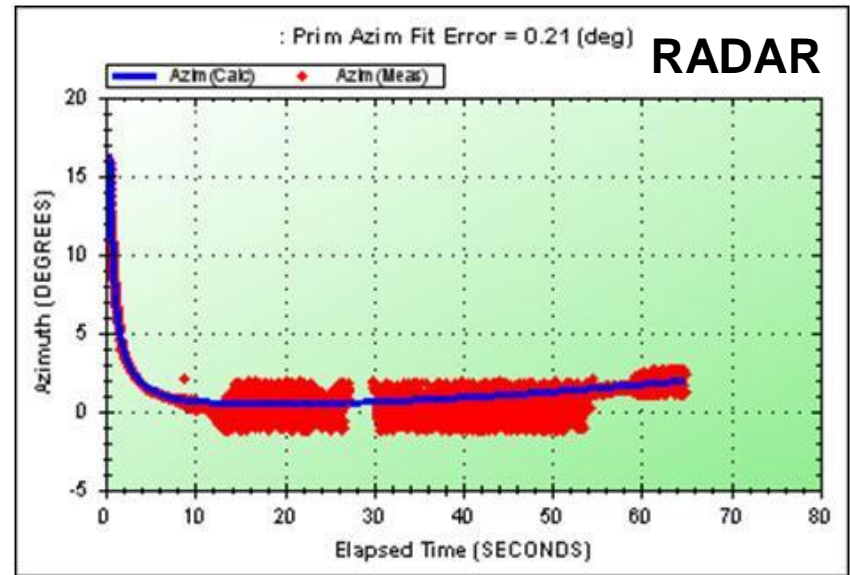
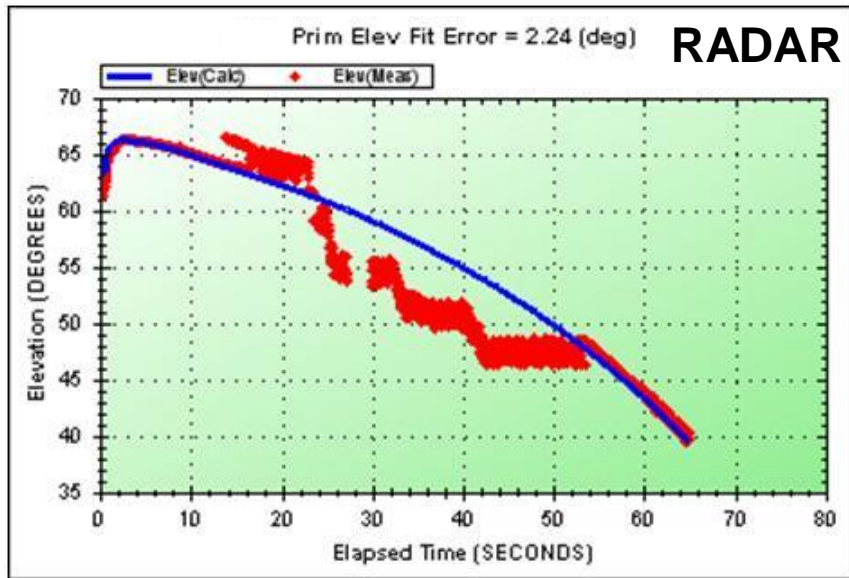


***Accelerations & Angular Rates yield information about Normal force coefficient & dynamic stability***

# KTM Camera Data



***KTM and Radar eliminates internal volume claims for telemetry, compresses schedules***



- **Improved Data Fusion**
  - Combining of sensor data from disparate sources
  - Improved Fit Accuracy
  - Use fewer KTM cameras to reduce test cost w/ equivalent accuracy
- **Provides Faster Turnaround of Final Results to Plan Next Test**
  - Increased Data Volume, helps narrow scope of subsequent testing
- **Feedback Loops Direct from Test to Design Activity**
  - Aerodynamics
  - Stability
  - Control Systems and Guidance and Sensors
- **Data reduction tools must be adaptable to include**
  - New data sources/instrumentation quickly
  - New control systems

***•Data Fusion provides maximum use of data from different instrumentation & improves aerodynamic determination, ensuring best use of limited available resources***