



U.S. Army Research, Development and Engineering Command



**Metrics Analysis
for the Improved Evaluation Methodology
of the Hazard Severity of Fragments
Projected from Deflagrating Warheads**

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Symposium & Exposition
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TECHNOLOGY DRIVEN. WARFIGHTER FOCUSED.

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Current Type IV Response Descriptor



Per MIL-STD-2105D / AOP-39(3):

- “At least **one piece** (e.g. casing, packaging, or energetic material) **travels** (or would have been capable of travelling) **beyond 15m and with an energy level greater than 20J** based on the distance versus mass relationships in figure 1.”
 - Where did 20J come from?
 - Why did we switch from 79J to 20J?
 - Why is 15m (50ft) significant?
 - Are these the best metrics?
 - What method are we using to measure these metrics?
 - Is there a better method to measure these metrics?

*Note:

- 79J in AOP-39 Ed 2 (2009) and MIL-STD-2105C (July 2003)
- 20J in AOP-39 Ed 3 (March 2010) and MIL-STD-2105D (April 2011)



Where did 20J & 79J come from?



Colonel Journee, French infantry officer established 15ft-lb & 58 ft-lb criterion in 1800's

- "Considered the **upper and lower bounds of what a man could endure from recoil of a rifle**".
 - **15 ft-lb (20J)** was set as the **maximum recoil suitable for a military rifle**
 - **58 ft-lb (79)** recoil energy was estimated to provide **significant bruising/damage to typical shoulder**

TOP 3-2-504 – Daily Firing limit for safety of hand and shoulder weapons

Weapon System	Muzzle Recoil Energy (ft-lbs)
Lee-Enfield Rifle	12.75 ft-lbs
.45 Cal. Rifle	14.40 ft-lbs
.30 Cal Garand	15.18 ft-lbs
Springfield '03 Rifle	14.98 ft-lbs

15 ft-lbs (20J) →
58 ft-lbs (79J) →

Computed Recoil Energy	Limitation
Less than 15 ft-lb (20.3 Joules)	Unlimited Firing
15-30 ft-lb (20.3 - 40.7 Joules)	200 rounds / day / shooter
30-45 ft-lb (40.7 - 61.0 Joules)	100 rounds / day / shooter
45-60 ft-lb (61.0 - 81.4 Joules)	25 rounds / day / shooter
Greater than 60 ft-lbs (81.4 Joules)	No Shoulder Firing

- » Shotguns produce 25 ft-lb to 35 ft-lb of recoil
- » Elephant gun produces ~ 52 ft-lb of recoil

"The recoil energy of the Lee-Enfield rifle is well below the maximum energy of recoil advisable for a military rifle, which should not exceed 15 foot pounds." --1909 British Textbook of Small Arms



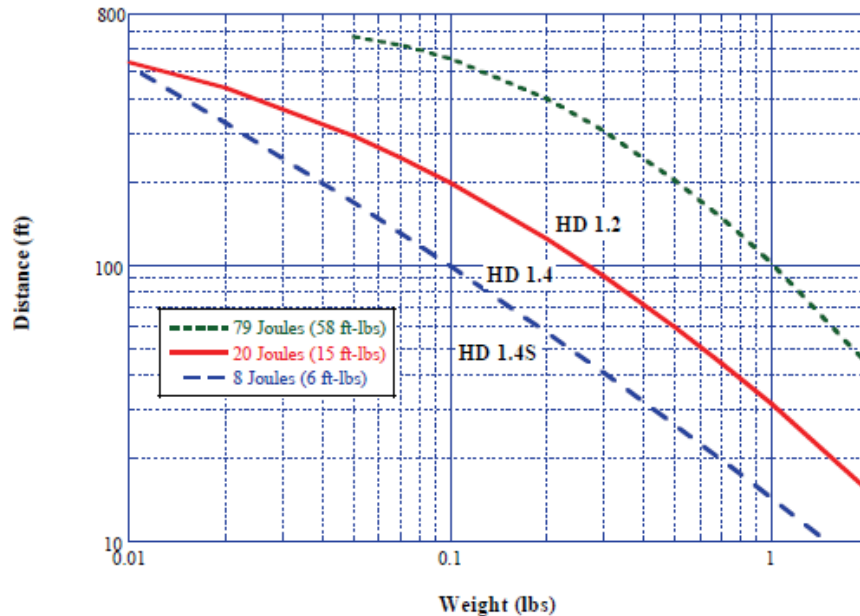
- Since then, 20J & 79J have been referenced and used for numerous applications
 - Testing standards, injury thresholds, toy/weapon limits, etc.
- Currently we use the fragment's mass and distance to calculate its energy.
 - Found that many projectiles are not lethal, or even very hazardous with 20J/79J.
- Examples of projectiles and their associated energy:
 - Paintball 300ft/s – **12J**
 - 0.177 cal pellet (air gun) 900ft/s– **21J**
 - Baseball 90mph – **120J**
 - 40mm non-lethal grenade 200ft/s – **150J**





TB 700-2

TB 700-2
NAVSEAINST 8020.8C/TO 11A-1-47



58 ft-lbs (79 J)

D in ft, M in lbs

$$D = 101.65 * M^{[-1.1061 - 0.15961 * \ln(M)]}$$

$$M = 4.24 * D^{[1.8714 - 1.2433 * (\ln(D)) + 0.25442 * (\ln(D))^2 - 0.018948 * (\ln(D))^3]}$$

D in m, M in kg

$$D = 11.697 * M^{[-1.35846 - 0.15961 * \ln(M)]}$$

$$M = 4.533 * D^{[0.132633 - 0.49695 * (\ln(D)) + 0.16437 * (\ln(D))^2 - 0.018948 * (\ln(D))^3]}$$

15 ft-lb (20 J)

D in ft, M in lbs

$$D = 31.49 * M^{[-0.98 - 0.0788 * \ln(M)]}$$

$$M = 0.000006151 * D^{[14.8843 - 6.0304 * (\ln(D)) + 1.0077 * (\ln(D))^2 - 0.06313 * (\ln(D))^3]}$$

D in m, M in kg

$$D = 4.212 * M^{[-1.103 - 0.0788 * \ln(M)]}$$

$$M = 0.1283 * D^{[4.399 - 2.973 * (\ln(D)) + 0.7077 * (\ln(D))^2 - 0.06313 * (\ln(D))^3]}$$

6 ft-lb (8 J)

D in ft, M in lbs

$$D = 14.41 * M^{[-0.896 - 0.0252 * \ln(M)]}$$

$$M = 7.2157 * D^{[0.6007 - 0.9509 * (\ln(D)) + 0.2155 * (\ln(D))^2 - 0.01758 * (\ln(D))^3]}$$

D in m, M in kg

$$D = 2.13 * M^{[-0.935 - 0.0252 * \ln(M)]}$$

$$M = 2.4193 * D^{[-0.8642 - 0.3317 * (\ln(D)) + 0.1319 * (\ln(D))^2 - 0.01758 * (\ln(D))^3]}$$

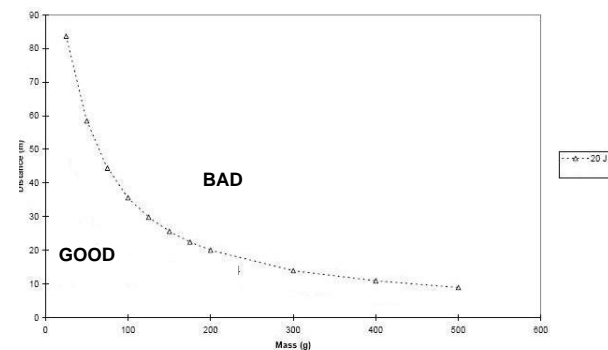
Figure 5-17

Relationship of Projection Kinetic Energy and Hazard Division



- Current Metric:
 - $E_{\text{Fragment}} > 20\text{J}$ beyond 15m \rightarrow TYPE IV
 - $E_{\text{Fragment}} < 20\text{J}$ beyond 15m \rightarrow TYPE V
- Current Method
 - Measurement of fragment location, orientation, weight, and condition.
 - **Mass and Distance** are then used to determine if fragment energy was over 20J.
 - *Handy frag energy calculator
 - If the fragment's energy is:
 - above the curve, TYPE IV
 - below the curve, TYPE V

Mass (g)	20 J	8 J
25	83.6	46.8
50	58.4	28.7
75	44.4	20.6
100	35.6	16.2
125	29.8	13.3
150	25.6	11.4
175	22.43	10
200	20	8.8
300	13.9	6.3
400	10.9	4.9
500	8.9	4.1





So what's the problem?

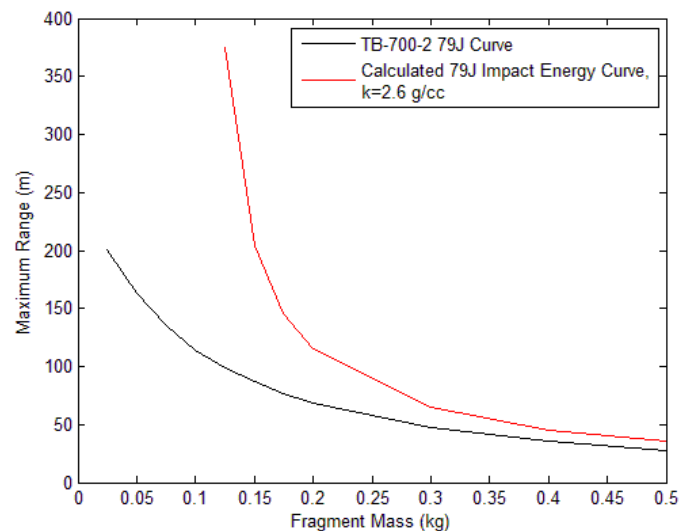
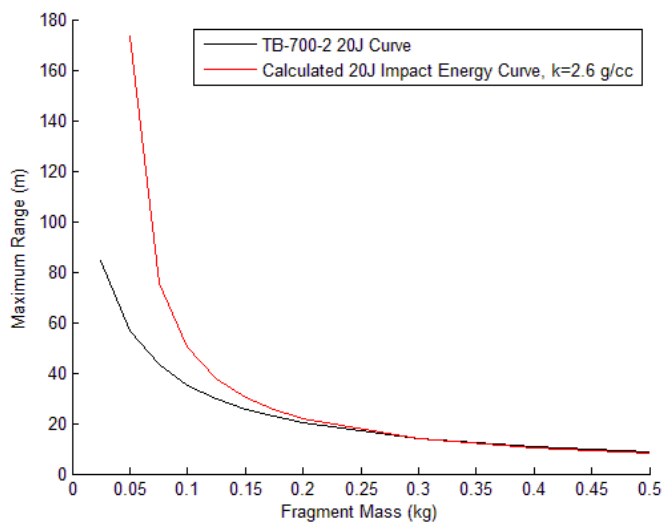


Problem #1:

- **Current curve** we use was formulated with a **Launch Energy Criterion**
 - Works based on **calculating max distance given mass can travel when launched with 20J.**
 - AOP-39 guidance indicates we measure Impact Energy.

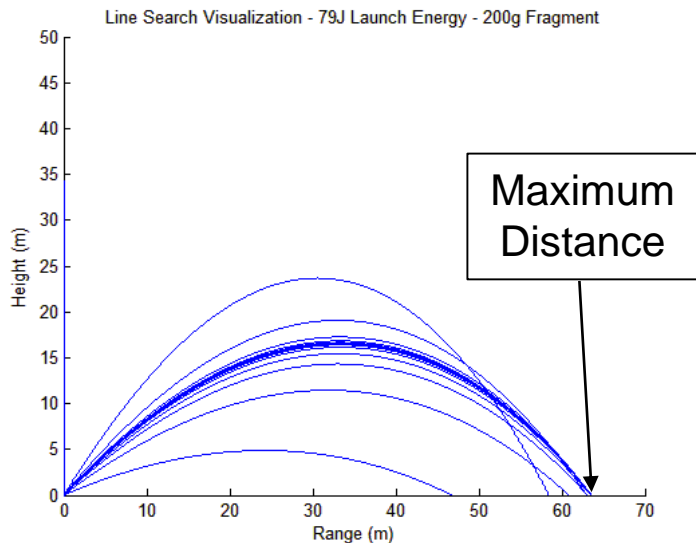
• Solution #1:

- We reformulated both curves (20J & 79 J) based on Impact Energy Criterion

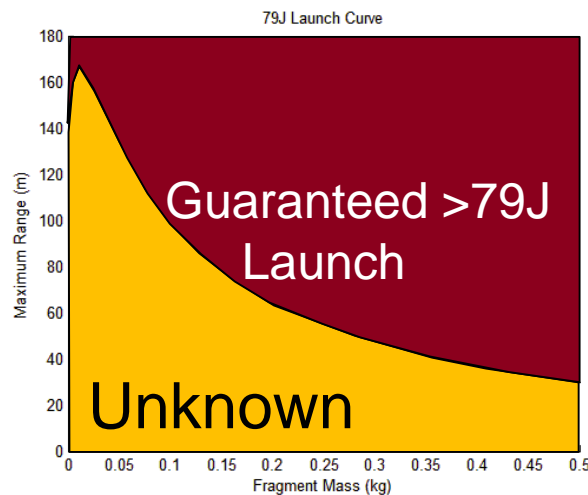
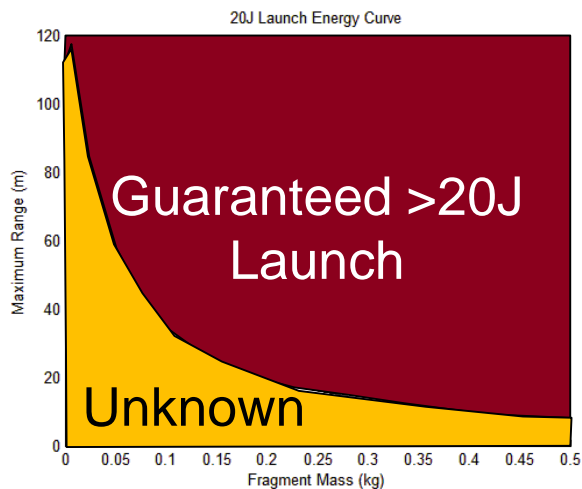




How does Launch Energy Criterion work?

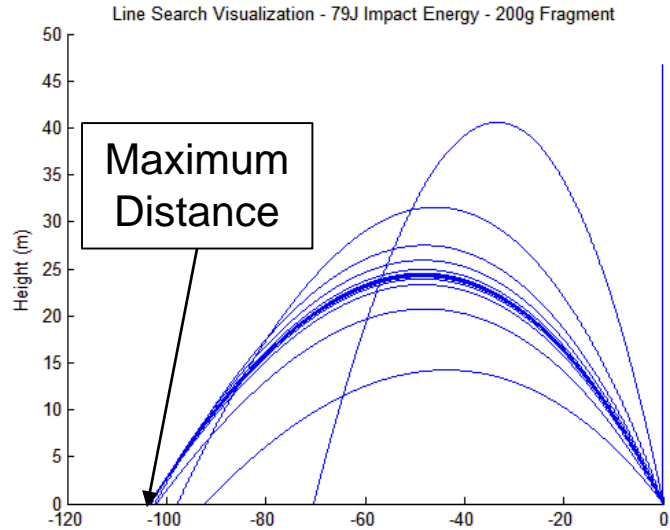


- Each point on the launch energy curves calculated using a line search forward in time from launch
 - Finds maximum distance a fragment of that mass could travel, having been launched at 20J
- Fragments that land past this distance are guaranteed hazardous
- Fragments that do not exceed this distance may or may not be hazardous
 - For example, high energy fragments launched vertically or directly at the ground
 - All curves calculated from starting height of zero. A starting height changes the curves!
 - Ricochet can be modeled (questionable accuracy)

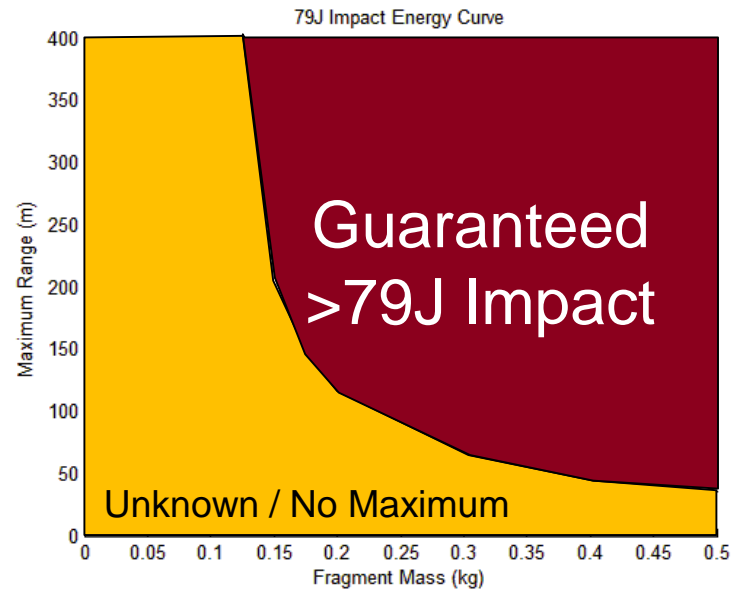
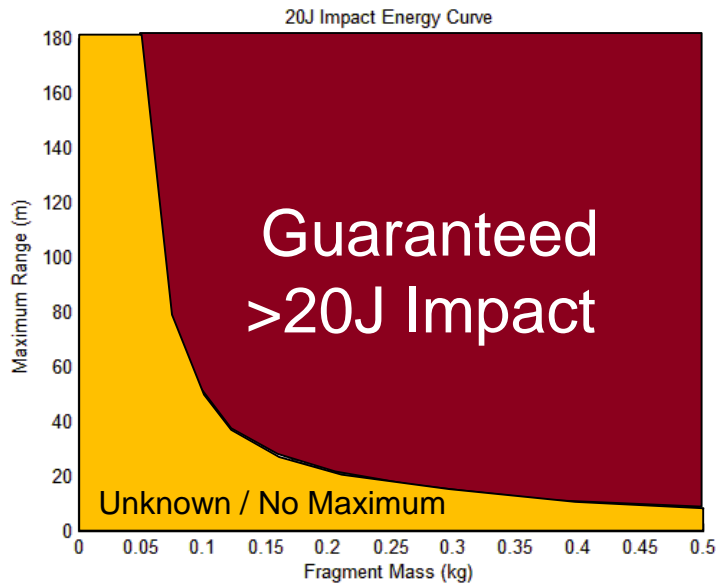




How does Impact Energy Criterion Work?



- Each point on the launch energy curves calculated using a line search backward in time from impact
 - Finds maximum distance a fragment of that mass could travel, having impacted at 20J
- Fragments that land past this distance are guaranteed hazardous
- Fragments that do not exceed this distance may or may not be hazardous
 - For example, high energy fragments launched vertically or directly at the ground
- The curve goes off to infinity for small fragments



What else is wrong with the curve?

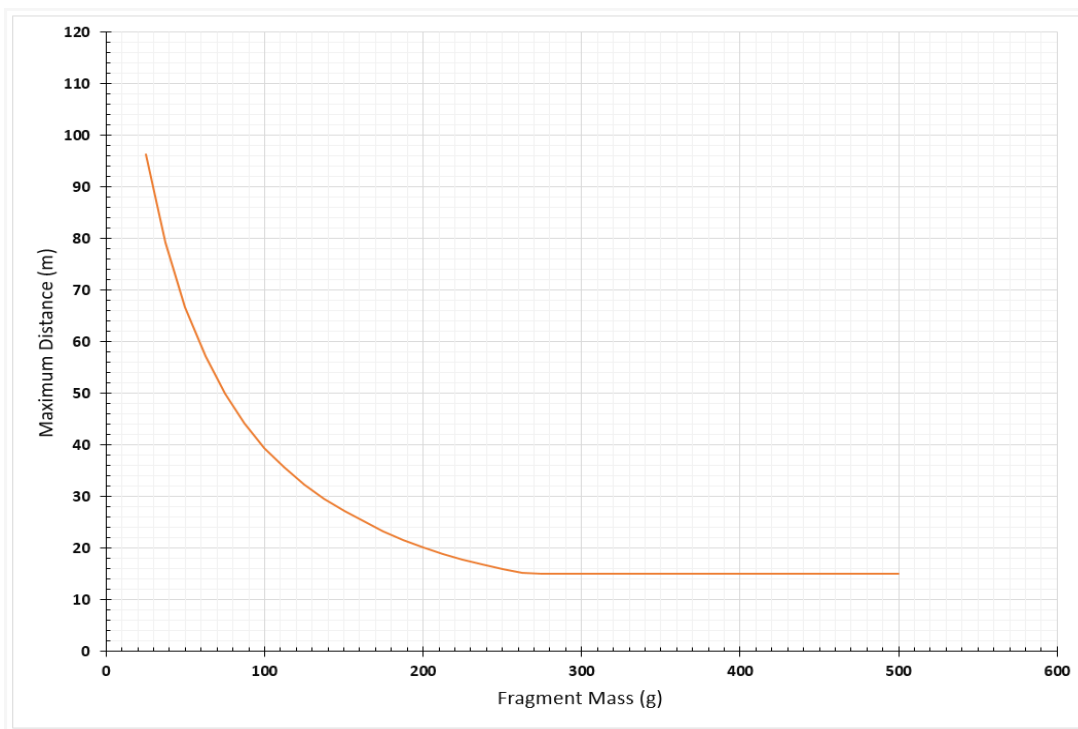


Problem #2:

- Current curve doesn't take into account 15m.

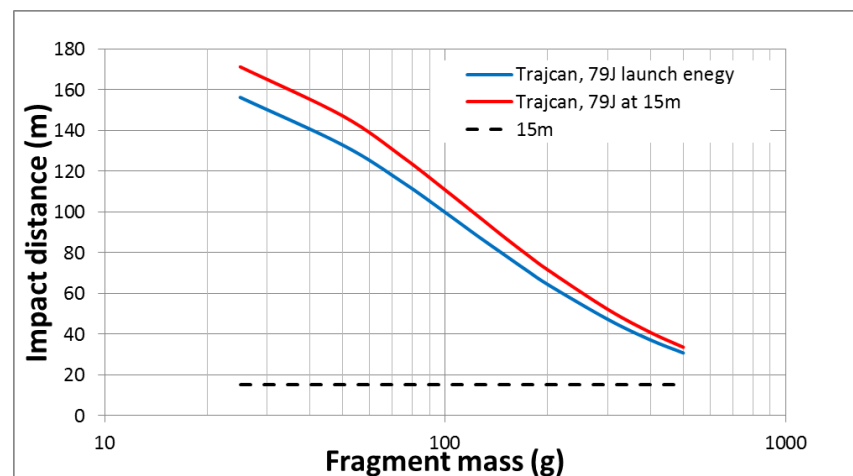
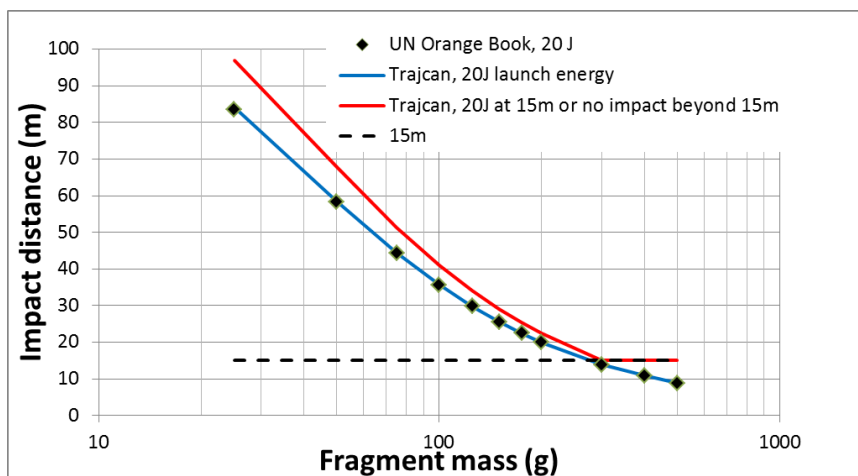
• Solution #2:

- Incorporated 15m in 20J Impact Energy @ 15m curve.





- **MSIAC TRAJCAN results agree**
 - Martijn Van der Voort incorporated 15m in 20J Impact Energy @ 15m curve.



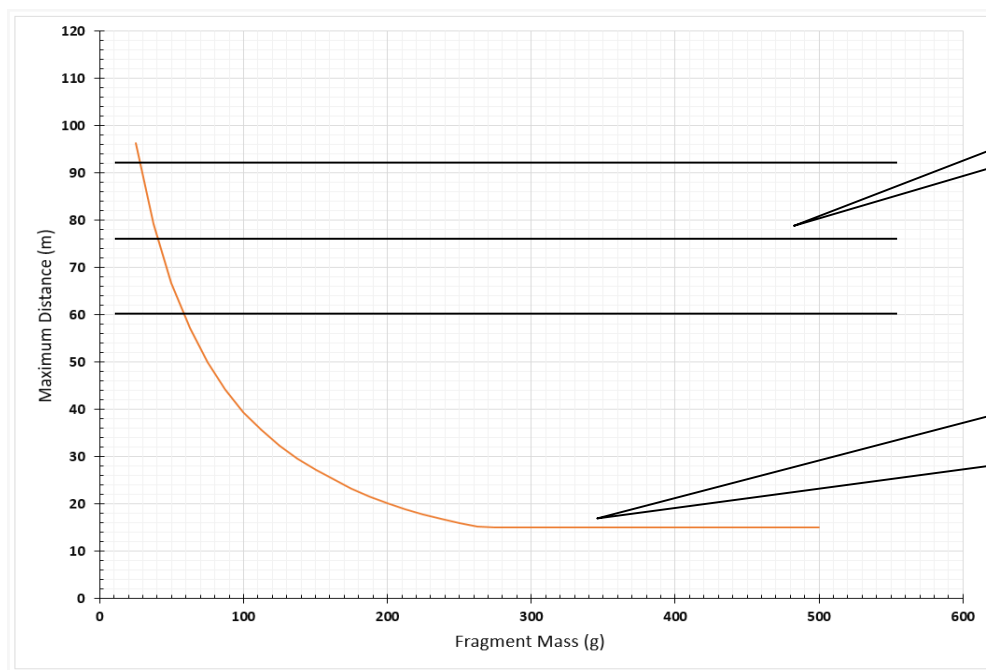
2016 INSENSITIVE MUNITIONS & ENERGETIC MATERIALS TECHNOLOGY SYMPOSIUM, NASHVILLE, TX, **PROJECTION CRITERIA FOR INSENSITIVE MUNITIONS AND HAZARD CLASSIFICATION**, Martijn M. van der Voort, Ernest L. Baker, Emmanuel Schultz and Michael W. Sharp, *Munitions Safety Information Analysis Center (NATO), Brussels, Belgium.*



What else is wrong with the curve?



- Curve still may not converge enough for Type IV/V fragments
 - Further investigation required to bound upper/lower limits
 - Potentially



Arbitrary lines represent potential 'ceiling' for non-Type IV/V frags

Flattens out due to masses so large that cannot impact with at least 20J by virtue of travelling 15m.

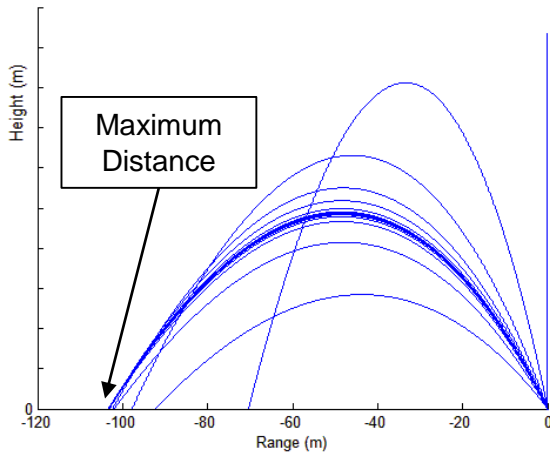


Impact Energy @ 15m:

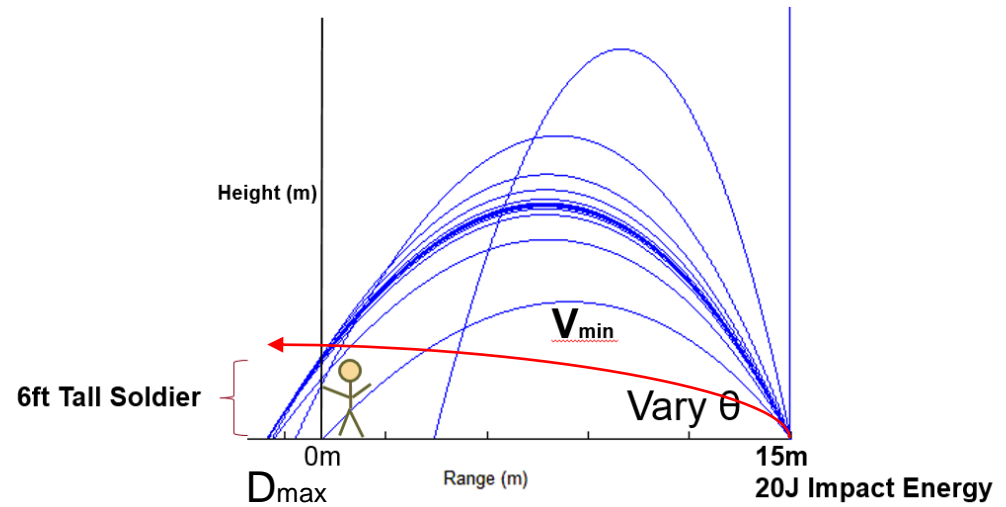
- Find V_{min} of 15m, 20J Impact
- Use V_{min} , Increase θ to find D_{max}
- Use D_{max} to find E_{max}

Conservative approach indicates 20J at 15m, Higher than 20J beyond 15m.

Impact Energy



Impact Energy @ 15m





Does that resolve all issues?

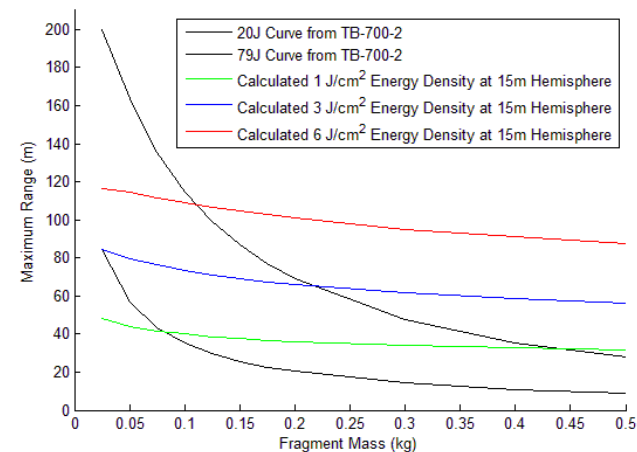


Problem #3

- Energy (J) alone is not a good measure of impact
 - Does not take into account the energy applied per the presented area
- Energy Density (J/cm^2) is a better measure of impact
 - Does take into account the energy applied per the presented area
- Example:
 - 32g, 2" diameter, object fired at 150fps produces 33.4J
 - 3.5g, 2" diameter, object fired at 230fps produces 8J
 - Both objects produce $\sim 3.8\text{J}/\text{cm}^2$
 - The key attribute is the presented area of the objects

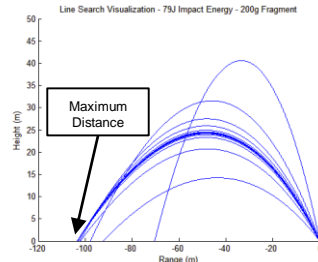
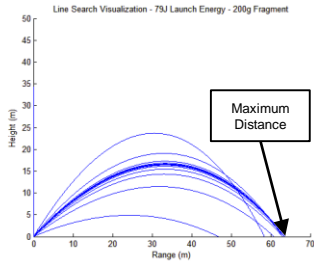
Solution:

- ARDEC formulated Energy Density curves for
 - $1\text{J}/\text{cm}^2$,
 - $3\text{J}/\text{cm}^2$
 - $6\text{J}/\text{cm}^2$

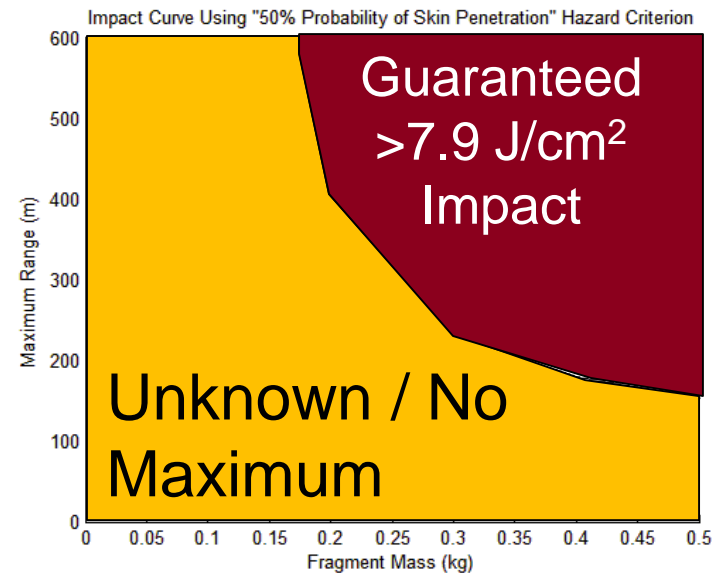
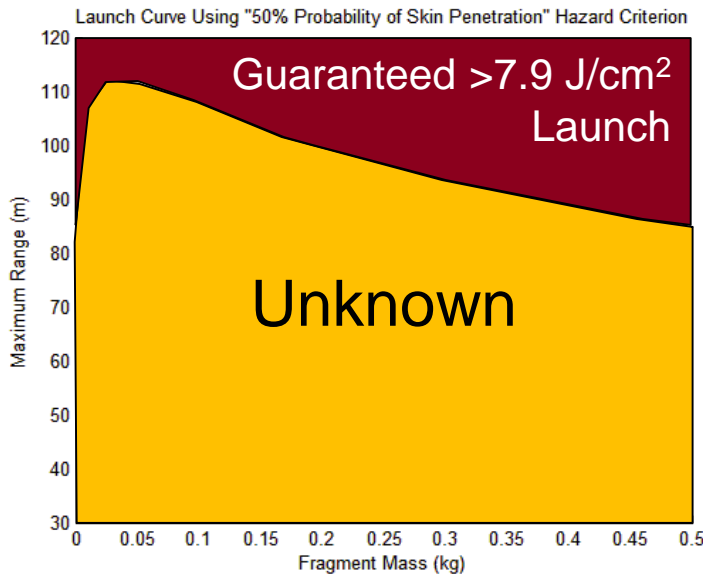




How does Energy Density Work?



- Energy Density can be used with either the:
 - Launch Energy Criterion or
 - Impact Energy Criterion
- Major difference is that mass is computed as a function of presented area:
 - $mass = k * (presented\ area)^{3/2}$
 - $k = 2600\ kg/m^3$
- The issue with using $7.9\ J/cm^2$, which is the 50% skin penetration model, distances are too large for IM purposes.





What is the solution?

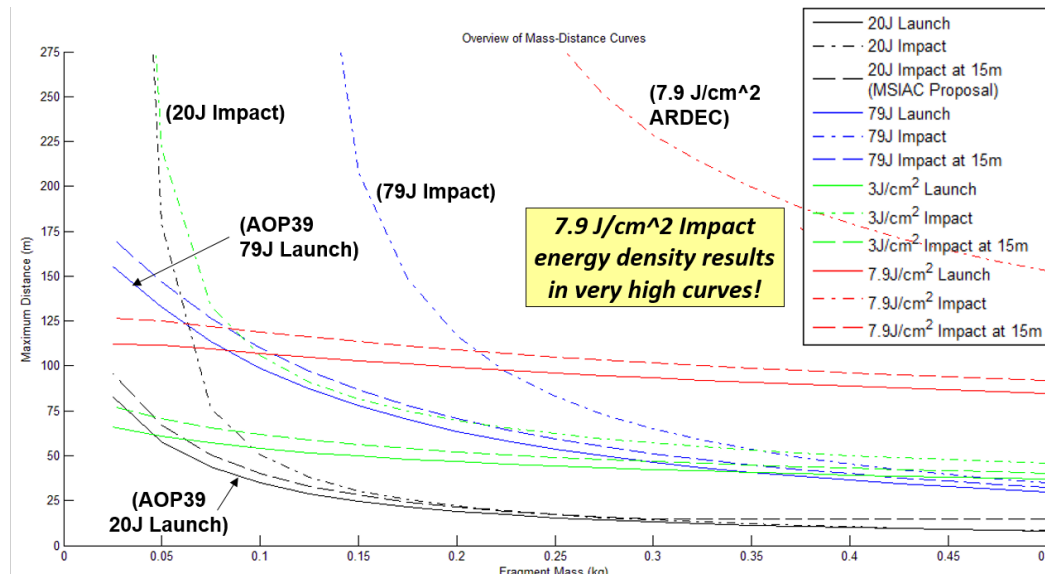


Problem #4:

- What is an **acceptable metric** for using the **Energy Density Criterion**?
- What is an appropriate metric to use as threshold for hazardous fragment in the realm of IM Type IV/V fragments?

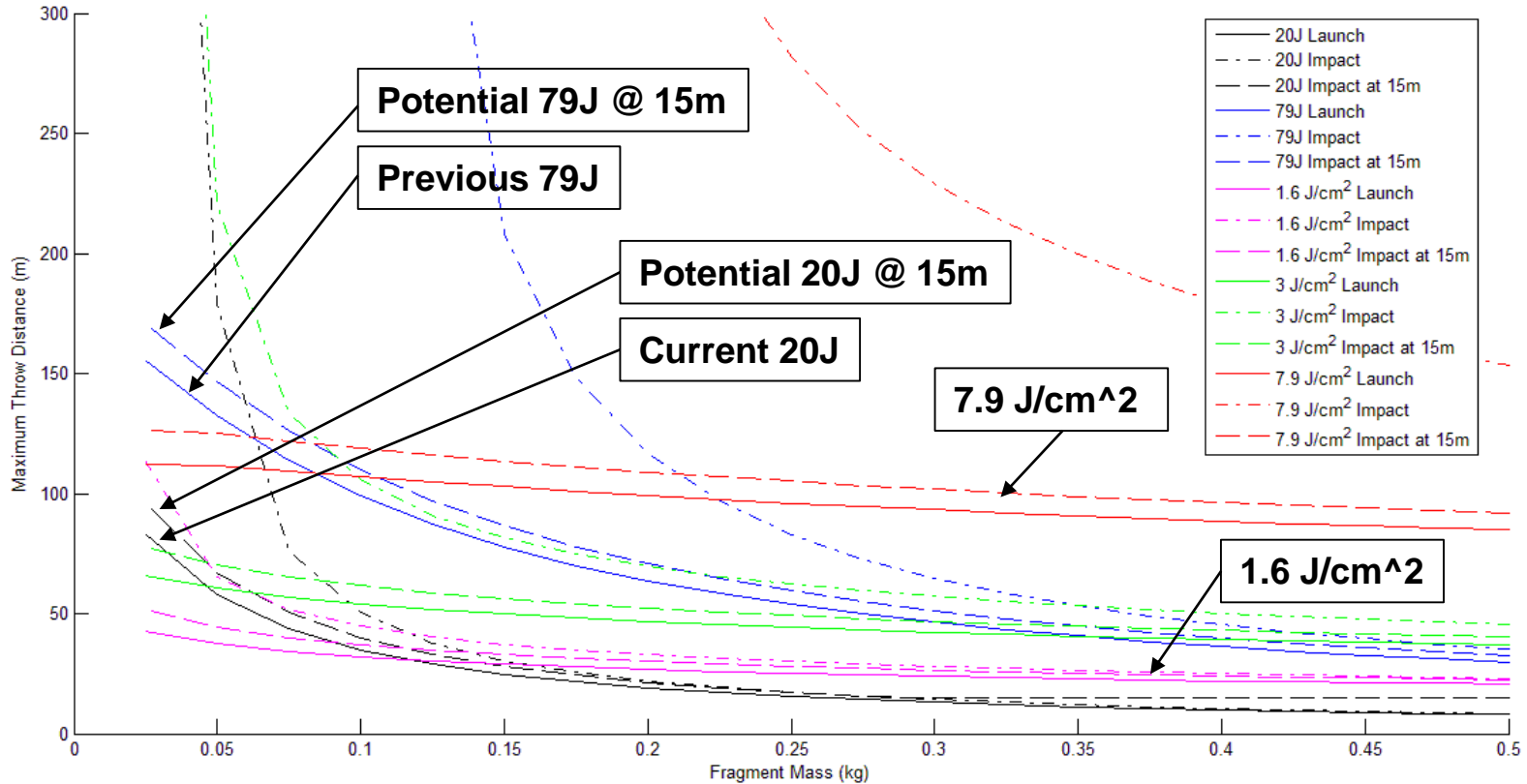
Solution #4:

- Lethality & safety experts suggest **7.9 J/cm²** is more relevant to **penetration injury/impacts**.
- Literature research suggests **1.6 J/cm²** appropriate for human injury based on “**Blunt Theory**”.





Comparison of Candidate Solutions



- Impact energy curves go off to infinity for small mass (terminal velocity)
- Impact energy at 15m curves are very close to launch energy curves



The Problem with Mass-Distance Curves



Curves represent a maximum throw distance

Above curve: Guaranteed hazardous (minimum energy to reach)

Below curve: NOT guaranteed safe! (high and low trajectories can ALWAYS deliver a hazardous fragment below curve)

distance

Pro: Less restrictive curve, more realistic lethality criterion, easier to pass

Con: “Uncertainty problem” - If all fragments fall below curve, no useful information is obtained – NOT guaranteed safe under the curve!

Pro: Less uncertainty – “Low probability you’re definitely in trouble”

Con: Easier to fail

mass



The Problem with Mass-Distance Curves

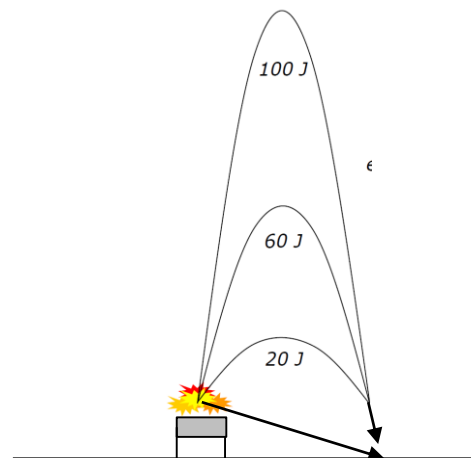
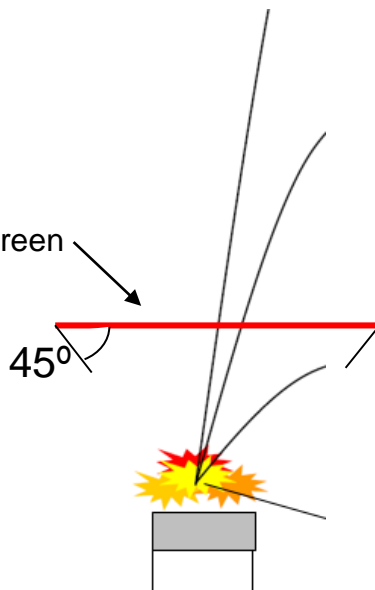


Risk: Frags under curve may have extremely high/low trajectories and may have travelled with high velocity/energy

Mitigation:

- Accept – We currently accept this risk
- Confirm trajectories utilizing equipment
 - HC witness screens
 - Cameras
 - Etc.

Example: HC Witness Screen





Portfolio of Curves



- Current curves assume chunky, tumbling, steel fragment
 - Not accurate evaluation for characteristic-unique fragments
 - Must consider other factors:
 - Density
 - Shape
 - Stability
 - Etc.
- Should be several curves to reference when evaluating unique fragment
- A set curves superimposed on one graph, each incorporating density, shape, and stability. User references specific curve for unique fragment.

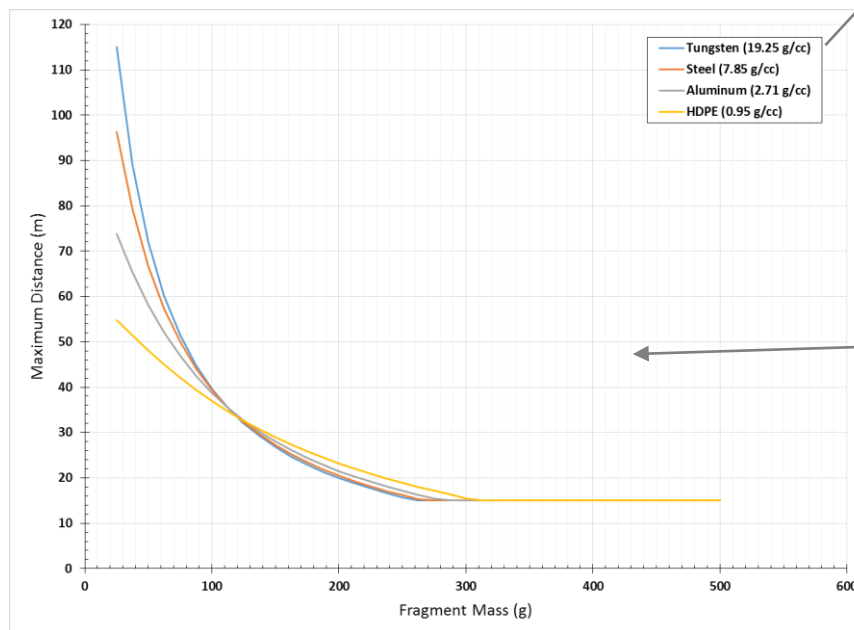


- For fragments of different density than steel, effect of drag can be taken into account using the previous methodology.

– Can group into four categories:

- $\frac{3}{4}$ density of steel
- $\frac{1}{2}$ density of steel
- $\frac{1}{4}$ density of steel

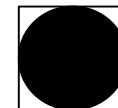
$$V = V_0 \exp\left(-\frac{\rho_{air} S C_D}{2m} x\right) = \sqrt{\frac{2E_0}{m}} \exp\left(-\frac{\rho_{air} \frac{3}{2} \left(\frac{m}{\rho_{frag}}\right)^{2/3} C_D}{2m} x\right)$$



*Curves provided to NATO IM Working Group for inclusion into revised AOP-39

- **Energy Density Methodology**

- *Impacting Surface Area of Fragment* must be accurately measured/assumed
- Not easy for asymmetric fragments
- Several methods proposed:
 - Automated 3-D optical measurement device – icosahedron
 - Generic fractional volume categories (frag-in-a-box)
 - Cubical fragment
 - » Cube occupies 4/4 of a cube's volume
 - Convex fragment
 - » Sphere ~3/4 of the cube's volume
 - Concave fragment
 - » Hour glass ~2/4 of the cube's volume.
 - Length/Diameter
 - » Long, thin rod/strip ~1/4 of the cube's volume.





Future Work – Metrics



- **Technically identify and justify Energy Density Methodology**

- Leverage with SMEs

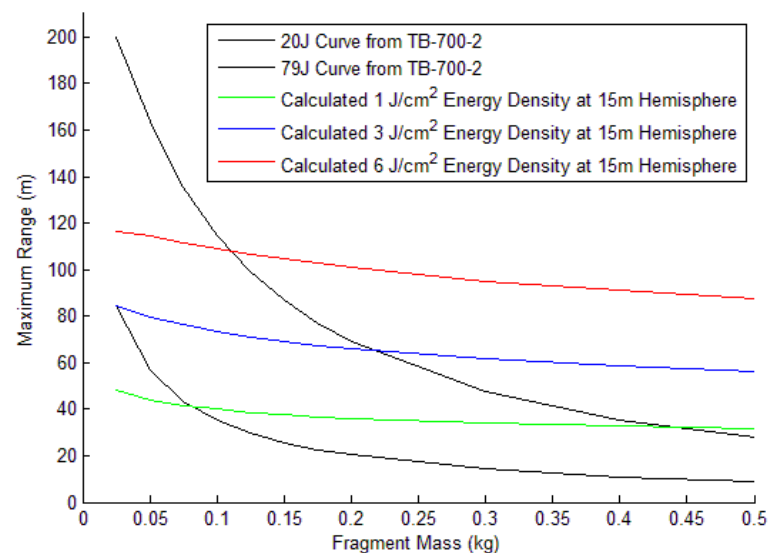
- ARDEC

- Aero ballisticians
- Lethality Division
- Non-Lethality Division
- System Effectiveness
- Biomedical Engineering

- TBRL

- ARL

- SLAAD





Conclusion



- Inherent issue with Mass-Distance curve for Pass/Fail Criteria
- Best we can do is fix current curve, and improve criteria
- ARDEC reformulated the curve with Impact Energy Criterion
- MSIAC reformulated Impact Energy Criterion @ 15m
 - Much more conservative approach than previous curve
- The 20J vs 79J argument is irrelevant
- Energy Density is better method to measure impacts/injury than energy alone
- Literature and Lethality Experts suggest 1.6 J/cm² for our IM realm of Type IV/V fragments / injuries
- NATO Response Descriptor Working Group (RDWG) Decision



Questions?



Back-up Slides



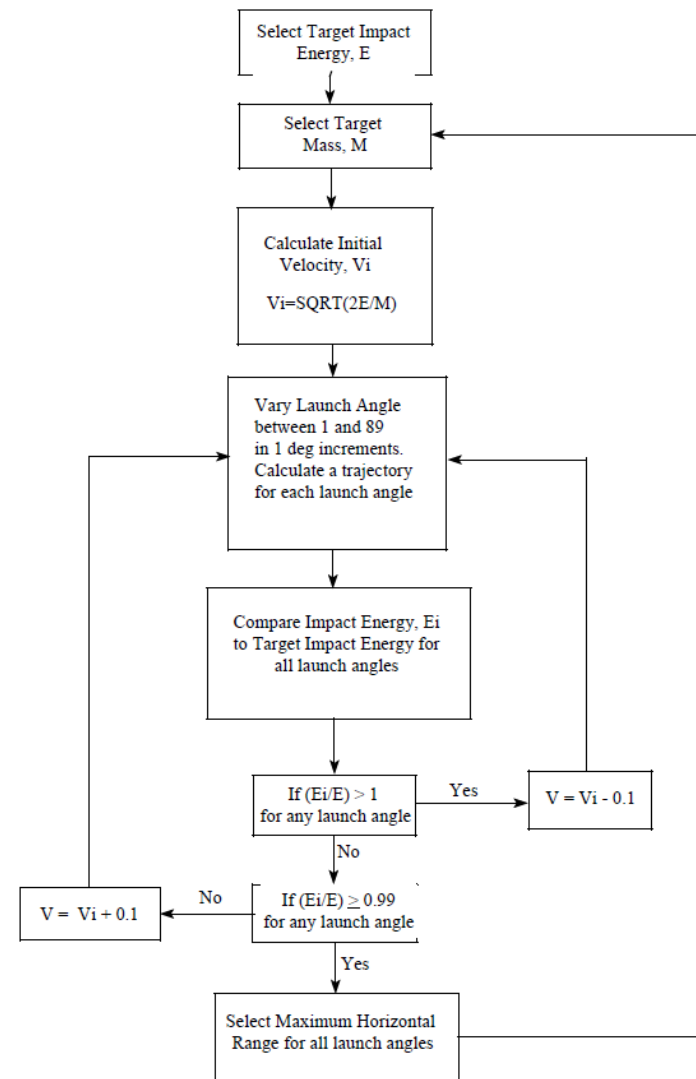


Status of Current Response Descriptors



- What are we currently doing?
 - “Type IV (Deflagration)” if fragments found further than TB-700-2 20J curve
 - We spoke to the originators of the TB-700-2 curves, were provided with the following methodology
 - See flow chart they provided
 - Limits the maximum impact energy to 20J
 - The maximum impact energy *is* the launch energy (unless item is on a stand)
 - “at 15m” caveat not considered in their calculation
 - The TB-700-2 20J curve definitely represents maximum distance a fragment could be thrown at 20J launch energy

The 20J and 79J curves in both TB-700-2 and the UN Orange Book represent launch energy as a result of a mistake in the calculations





Equations of Motion
(Vector Form)

$$\frac{d\mathbf{V}}{dt} = -\frac{\rho S C_D}{2m} |\mathbf{V}| \mathbf{V} + \mathbf{g}$$

$$\frac{d\mathbf{x}}{dt} = \mathbf{V}$$

F=ma with air drag

$$\frac{dV_x}{dt} = -\frac{\rho S C_D}{2m} V V_x = -\frac{\rho S C_D}{2m} V_x \sqrt{V_x^2 + V_y^2}$$

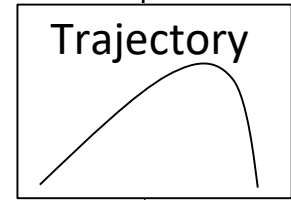
$$\frac{dV_y}{dt} = -\frac{\rho S C_D}{2m} V V_y - g = -\frac{\rho S C_D}{2m} V_y \sqrt{V_x^2 + V_y^2} - g$$

$$\frac{dx}{dt} = V_x$$

$$\frac{dy}{dt} = V_y$$

Equations of Motion
(Scalar Form)

Curve
Generation /
Other Analysis



(Modeling approximations)

Shape factor data

$$m = kS^{3/2}$$

If the fragments from a given weapon are assumed to be geometrically similar, the mass m and presented area A are related by $m = kA^{3/2}$. Values of k , called a shape factor or ballistic density, may be determined from weight and presented area measurements on fragments recovered from tests of particular weapons. Although the value of k differs from one weapon to another, for forged steel projectiles and fragmentation bombs the average value of 660 grains/in.³ (2.60 g/cm³) has been recommended, while for demolition bombs the value 590 grains/in.³ (2.33 g/cm³) has been applied.

(from Zaker, DDESB-TP-12)

(2.60 g/cm³)

Drag Coefficient Data

TABLE I DRAG COEFFICIENTS FOR IRREGULAR FRAGMENTS

MACH NUMBER	DRAG COEFFICIENT
0	0.80
0.75	0.88
0.90	1.09
1.15	1.26
2.00	1.14
4.00	1.08
>4.00	1.08

Note: Drag coefficient varies linearly between Mach Number entries

In Design Considerations for Toxic Chemical and Explosives Facilities; Scott, Ralph A., et al.; ACS Symposium Series; American Chemical Society: Washington, DC, 1987.

(from Swisdak, "Fragmentation Effects: An Overview")

- Numerical Solver
- MATLAB ode45 (variable-timestep Runge-Kutta)
 - Validate with flat fire solutions / ensure same results obtained for very small constant timestep
 - Can run backwards or forwards in time
 - Launch height usually zero
 - Stop integration when trajectory ordinate becomes negative

Ballistic trajectory calculations like these are where the TB-700-2 curves came from

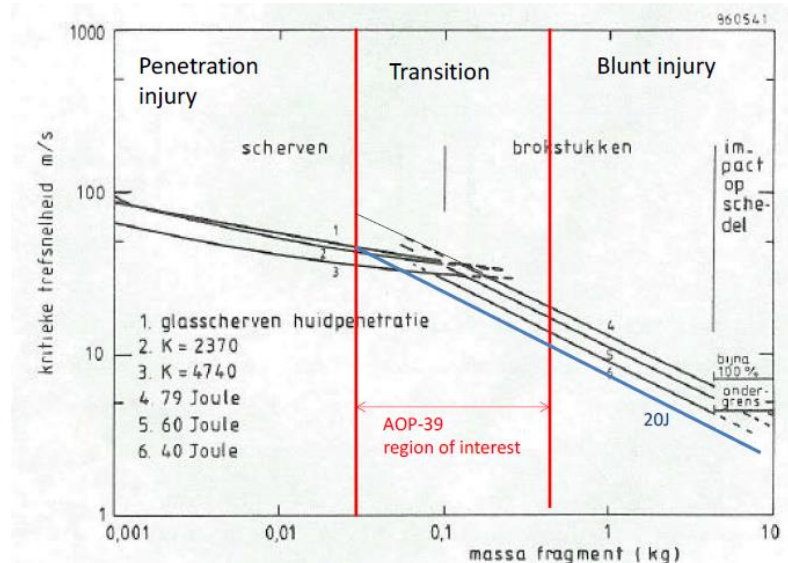


Skin Penetration vs. Blunt Trauma



- According to MSIAC:
 - Energy/Area more relevant for skin penetration
 - Energy more relevant for blunt trauma
 - Fragments in region of interest are big enough to start causing blunt trauma injuries at relatively low velocities
 - Furthermore, blunt trauma injuries will be caused at lower velocities thus a skin penetration criterion is not conservative

- It is conceivable that steel fragments of the sizes in AOP-39 can be thought of as relatively dangerous at relatively slow speeds
- Intuitive considerations regarding absorption of the impact energy
 - Partitioning of impact energy between projectile and target (energy absorbing structural deformation)
 - Distribution of force over impact surface
- US lethality experts should be consulted on what criterion makes sense for the fragments in this range



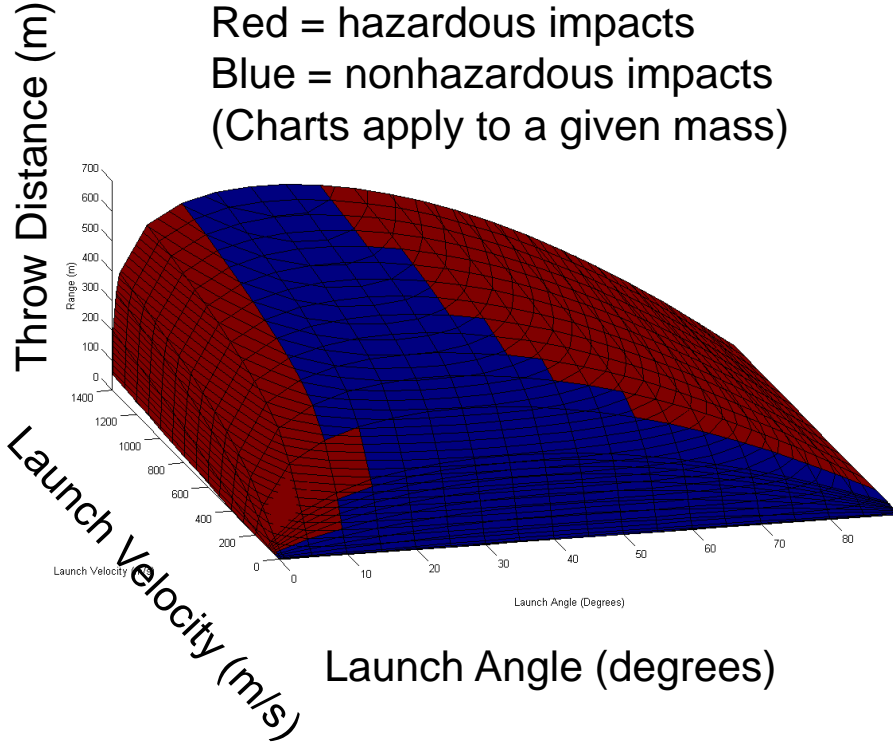
From Martijn van der Voort, "ANALYSIS OF THE IM TYPE V RESPONSE DESCRIPTOR"



Impact Energy at 15m (MSIAC Proposal) (Cont'd)

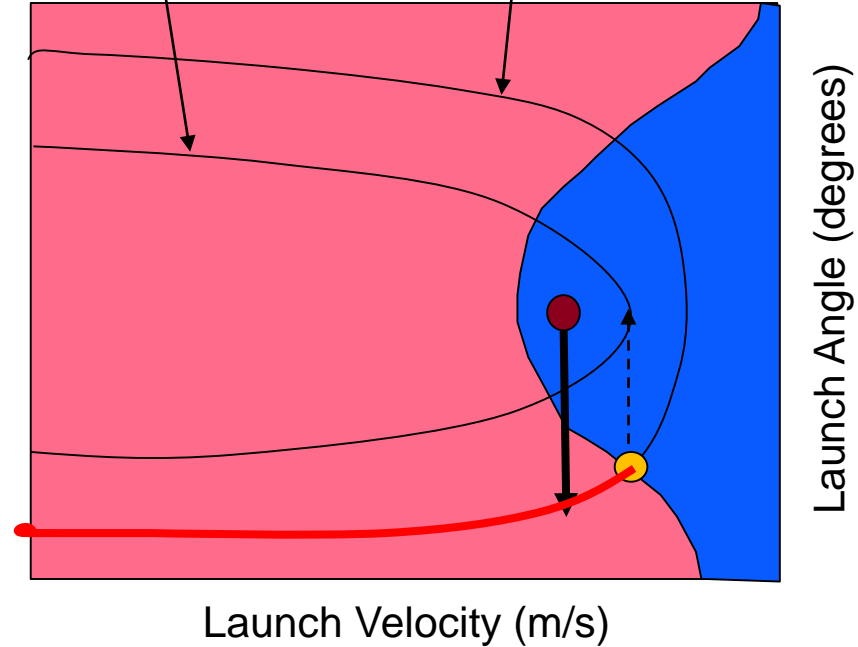


Red = hazardous impacts
Blue = nonhazardous impacts
(Charts apply to a given mass)



Range > 15m
contour (point on the
mass-distance curve)

Range=15m contour

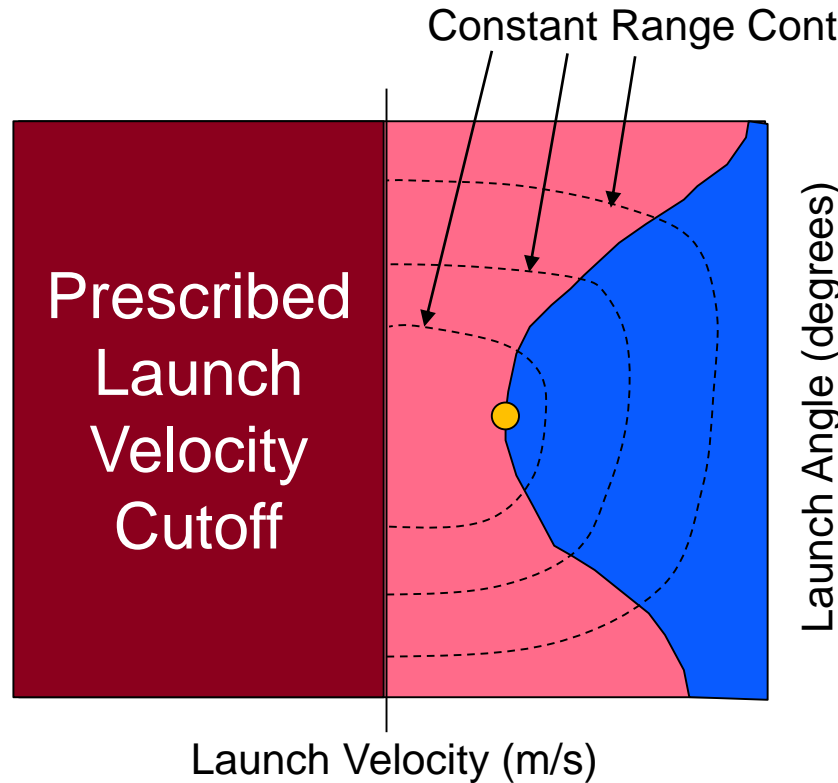


- Minimum velocity for hazardous impact at 15m
- Fragment found above MSIAC proposed curve
- Hazardous Impacts
- Non-Hazardous Impacts

Fragments which land above MSIAC curve are guaranteed to hit 15m with a hazardous fragment if the launch angle were lowered



Uncertainty Reduction Strategies - Probability Methodology



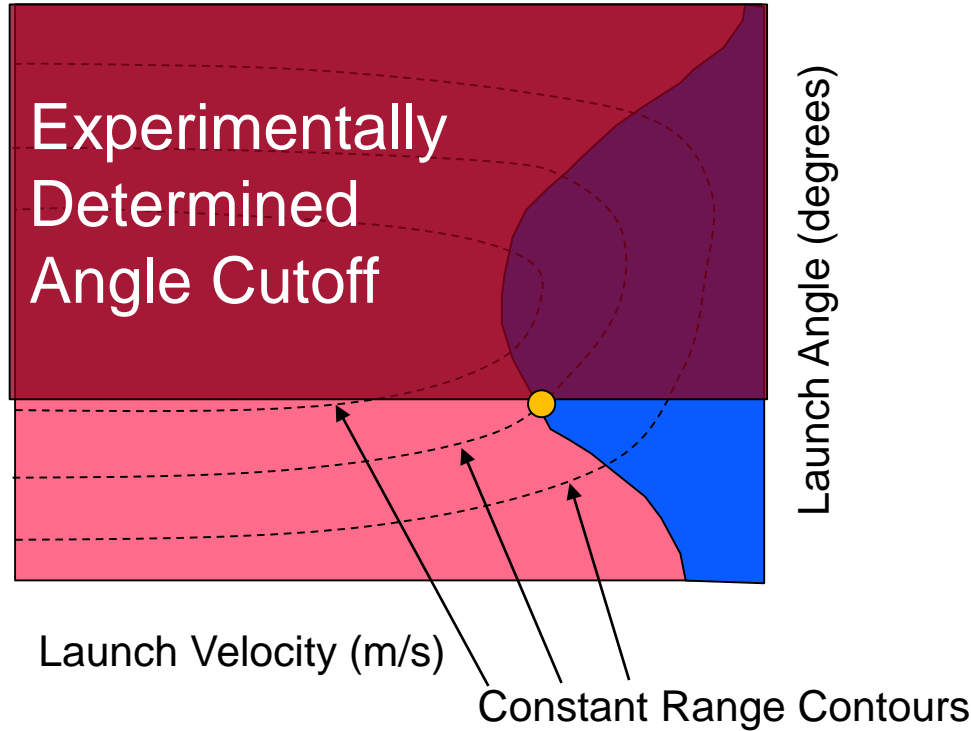
Fragments just under the curve have a (quantifiable) higher probability of being hazardous than fragments further below the curve

- Point used for impact mass-distance curve
- Impacts Not Considered
- Hazardous Impacts
- Non-Hazardous Impacts

Probability that a fragment under the curve is hazardous can be computed (~ratio of areas) if a launch velocity cutoff is prescribed and all trajectories equally likely



Uncertainty Reduction Strategies - Angle Cutoffs (Experimental)



Perhaps orthogonal cameras or witness screens of some sort could provide angle/velocity cutoff information

If it can be photographically determined that the largest launch angle out of all the debris does not exceed a given value, the curve is lowered (fidelity of the measurement is gained)

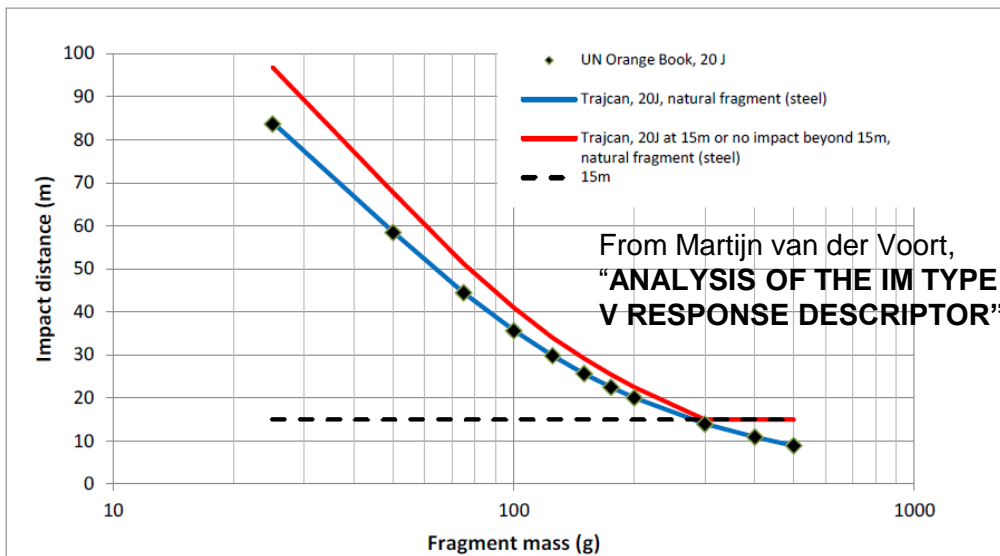
- New lower point used for impact mass-distance curve
- Impacts Not Considered
- Hazardous Impacts
- Non-Hazardous Impacts



Impact Energy at 15m (MSIAC Proposal) (Cont'd)



- MSIAC proposal is an **impact energy at 15m** criterion
 - This is different from an **impact energy** criterion (e.g., doesn't go off to infinity)
- Methodology
 - Find minimum possible launch velocity to hit person standing at 15m with a 20J impact
 - Using that velocity, adjust the launch angle until the maximum distance is found, this is the point used for their mass-distance curve
 - A fragment which lands above their curve has a higher velocity than the minimum velocity possible to reach a person standing at 15m with 20J
 - Therefore it **guarantees a person at 15m would be hit with at least 20J if the launch angle were lowered**



Pro: Guarantees hazardous impact at 15m if above curve, conservative lethality criterion reduces unknown region below curve

Con: Not much different from launch energy, lethality criterion may be too conservative